

AUTONOMOUS MOBILITY-ON-DEMAND SYSTEMS AND THE BUILT ENVIRONMENT: MODELS AND LARGE-SCALE COORDINATION ALGORITHMS

Federico Rossi
Advisor: Prof. Marco Pavone
Stanford, January 18, 2017

Self-driving vehicles

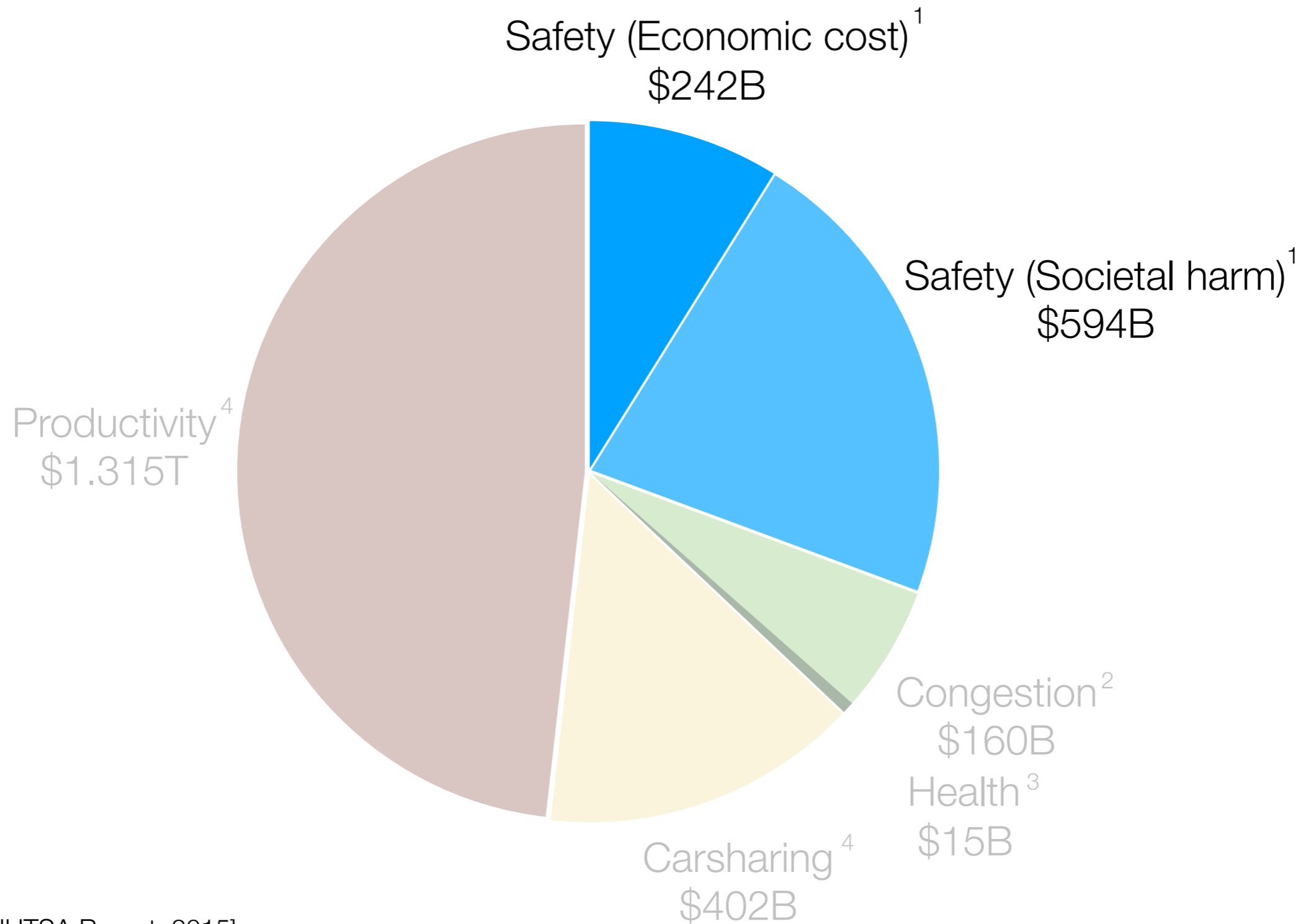


2005



2017

Self-driving vehicles



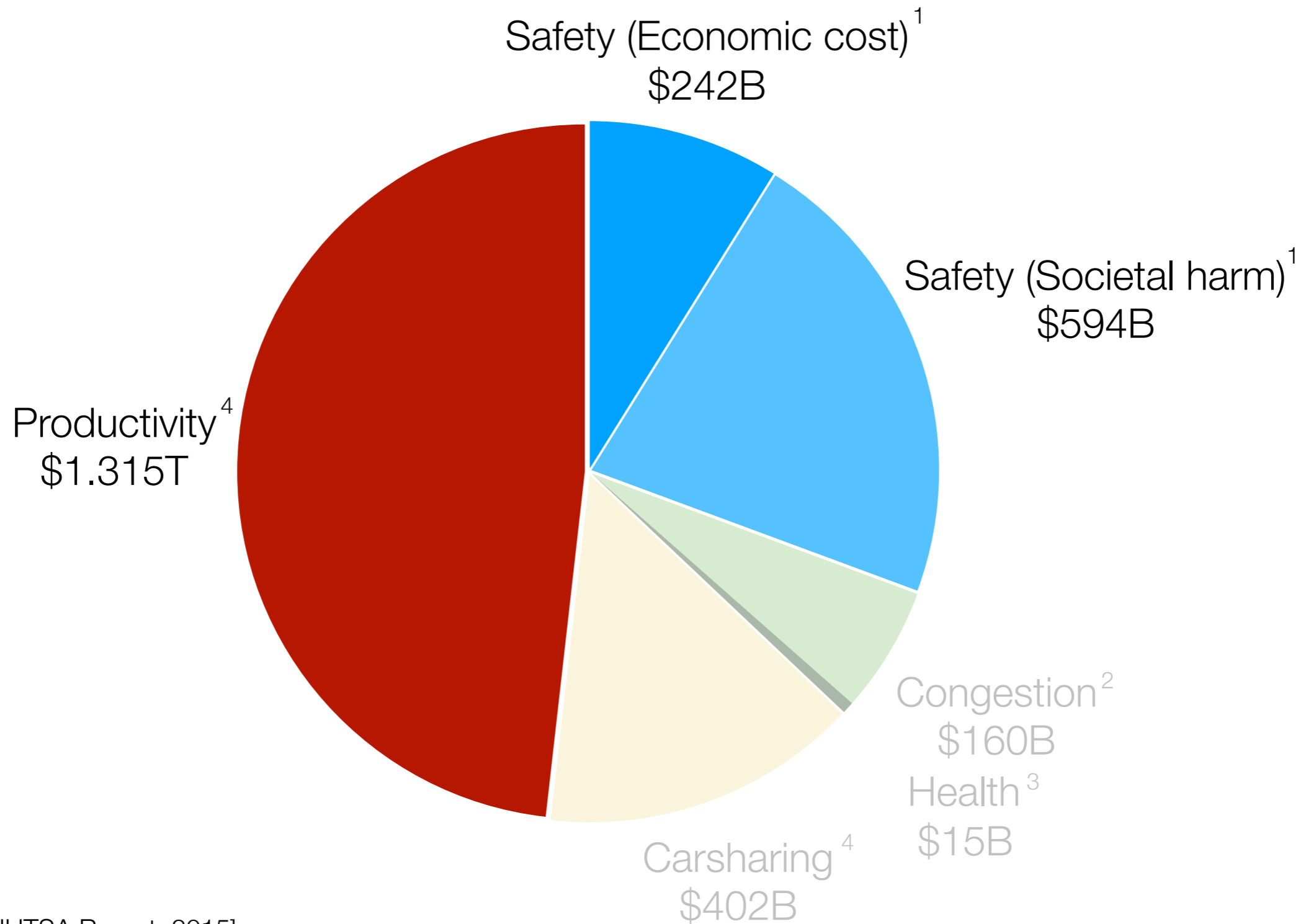
¹ [Blincoe et al., NHTSA Report, 2015]

² [Schrang et al., Texas A&M Transportation Institute, 2015]

³ [Levy et al., Environmental Health, 2010]

⁴ [Spieser, Treleaven, Zhang, Frazzoli, Morton, Pavone, Road Vehicle Automation, 2014]

Self-driving vehicles



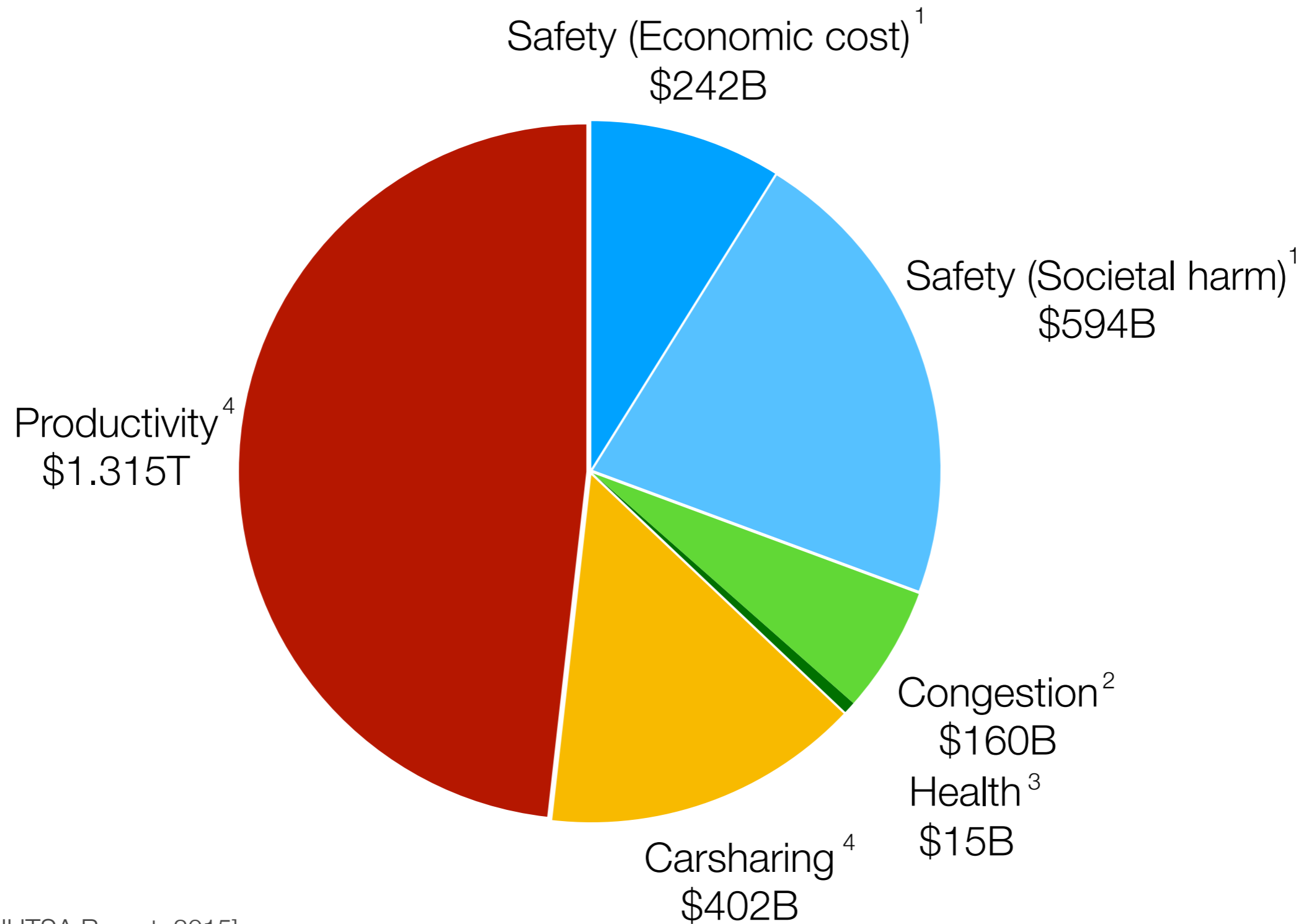
¹ [Blincoe et al., NHTSA Report, 2015]

² [Schrang et al., Texas A&M Transportation Institute, 2015]

³ [Levy et al., Environmental Health, 2010]

⁴ [Spieser, Treleaven, Zhang, Frazzoli, Morton, Pavone, Road Vehicle Automation, 2014]

Fleets of self-driving vehicles



¹ [Blincoe et al., NHTSA Report, 2015]

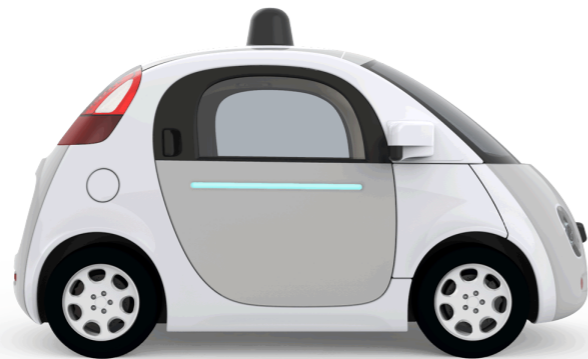
² [Schrang et al., Texas A&M Transportation Institute, 2015]

³ [Levy et al., Environmental Health, 2010]

⁴ [Spieser, Treleaven, Zhang, Frazzoli, Morton, Pavone, Road Vehicle Automation, 2014]

Autonomous Mobility-on-Demand

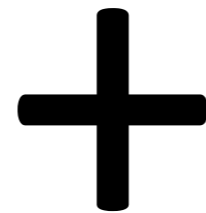
Vehicle Autonomy



Car Sharing



U B E R



Impact on the built environment?

AMoD systems and the built environment

- **Congestion**

“... the additional empty repositioning trips made by [shared autonomous vehicles] **increased congestion** and travel times and a significant number of [shared autonomous vehicles] were needed to provide effective service.”

[Levin et al. 2016]

“Robocars present one risk of increased congestion, because they allow vehicles to move while empty. ... Empty vehicles can **increase congestion.**”

– Brad Templeton

- **The electric power network**

“Depending on the scenario, price may increase by only 1.2–2.7 percent (in WECC – RMP/ANM) or, for evening recharging at 6 kW, by as much as 141 percent (in FRCC), 196 percent (in WECC-CA) and 297 percent (in SERC). In contrast to what was suggested by other research, the model predicts **increases in electricity prices** for **almost all regions.**”

[Hadley and Tsvetkova 2009]

“V2G could **stabilize large-scale** (one-half of US electricity) **wind power** with 3% of the fleet dedicated to regulation for wind, plus 8–38% of the fleet providing operating reserves or storage for wind.”

[Kempton and Tomic 2005]

Problem statement

- Propose **models** that capture the the **interaction** between AMoD systems and the **built environment**, with particular attention to traffic congestion and the electric power network.
- Propose **control algorithms** that optimize the performance of such AMoD systems.
- Validate these algorithms with **case studies** with real-world data.

In the literature

Control of AMoD systems

- Queueing-theoretical models [Zhang et al. 2014; Zhang et al. 2015; Calafiore et al. 2017]
- Dynamic vehicle routing models [Psaraftis '88; Berbeglia, Cordeau, Laporte '10; Pavone '10; Pavone et al. 2011; Treleaven, Pavone, Frazzoli '13; Spieser et al. '14]
- Fluidic models [Pavone et al. 2012; Levin 2017]

No interaction with the built environment

In the literature

Traffic congestion

No optimization

- Traffic modeling:
 - Static models [Wardrop 1952]
 - Simulation models [Treiber, Hennecke, Helbing, 2000; Maciejewski 2017; Fagnant et al. 2014, 2016]
 - Queueing models [Osorio, Bierlaire, 2009]

- Dynamic Traffic Assignment (DTA) and System-Optimal DTA [Janson 1991]

No rebalancing

In the literature

EVs and the power network

- Scheduling charging [Rotering and Ilic 2011; Turitsyn et al. 2010; Tushar et al. 2012]
- Location of charging stations [Goeke and Schneider 2015; Pourazarm et al. 2016]

No feedback

- Macroeconomic effect of EVs [Hadley and Tsvetkova 2009]
- Game-theoretical models [Sioshansi 2012; Wang et al. 2010]

No spatial model

- Joint routing, charging, and economic dispatch [Alizadeh et al. 2016; Khodayar et al. 2013]

Private vehicles

Contribution

- Will AMoD systems increase urban congestion?

Not if properly **routed** [Zhang*, Rossi* and Pavone 2016a, Robotics: Science and Systems; Rossi et al. 2017, Autonomous Robots, in press.]

- Will fleets of electric vehicles help control the power network?

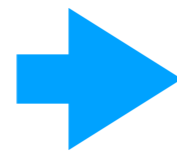
Yes, if properly **coordinated** [Rossi et al., in preparation for RSS 2018]

Other contributions

- Randomised algorithms for efficient routing in AMoD systems
- Model-predictive control of AMoD fleets with charging constraints [Zhang, Rossi and Pavone 2016b, ICRA]
- BMPC queuing-theoretical models of AMoD systems [Iglesias et al. 2016 WAFR; Iglesias et al. 2018, submitted to the International Journal of Robotics Research]
- Data-driven control of AMoD systems with LSTM estimation of customer demand [Iglesias et al. 2018, ICRA]

Network flow model

- Highly scalable (LP)
- Very expressive
- No stochasticity
- Continuum approximation



Expectation of a stochastic process

Flow decomposition and sampling

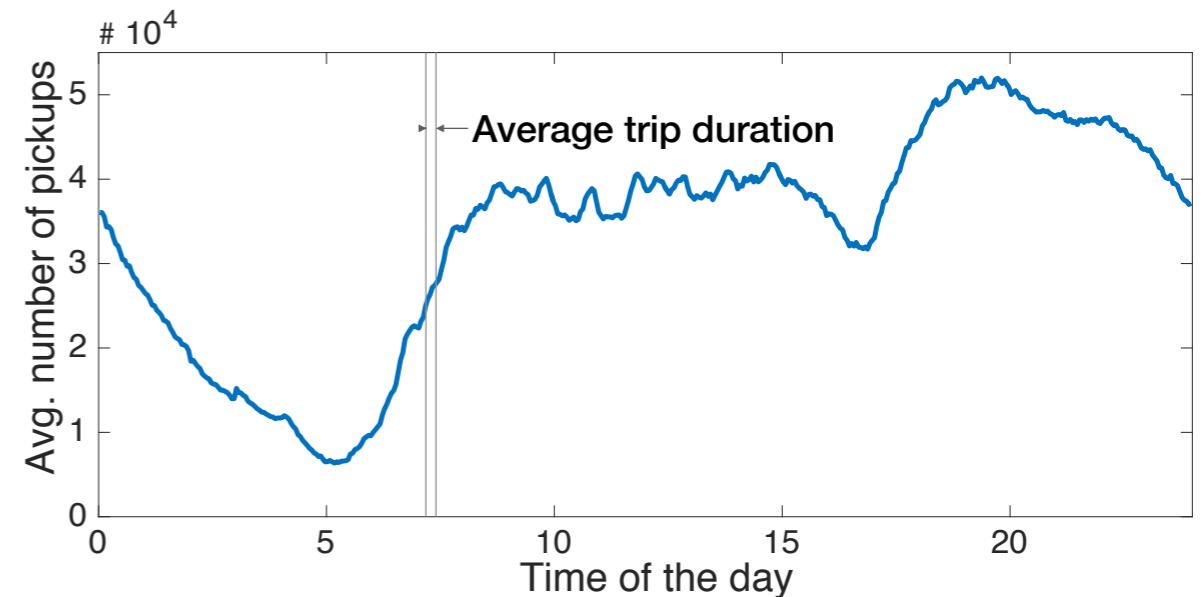
A map of a city street grid with a network of colored lines and dots overlaid. The lines are primarily purple and blue, with some red and green lines. The dots are small green circles. The text "PART I" and "AMoD SYSTEMS AND CONGESTION" is overlaid on the map.

PART I

AMoD SYSTEMS AND CONGESTION

Our approach: assumptions

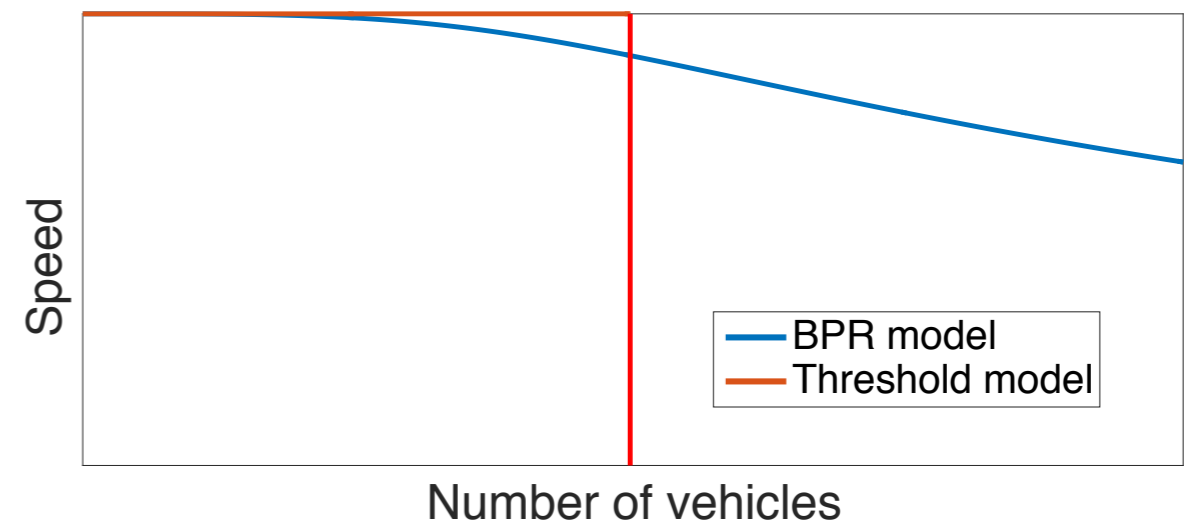
Customer demand is **time-invariant**



The road network is **node-symmetric**

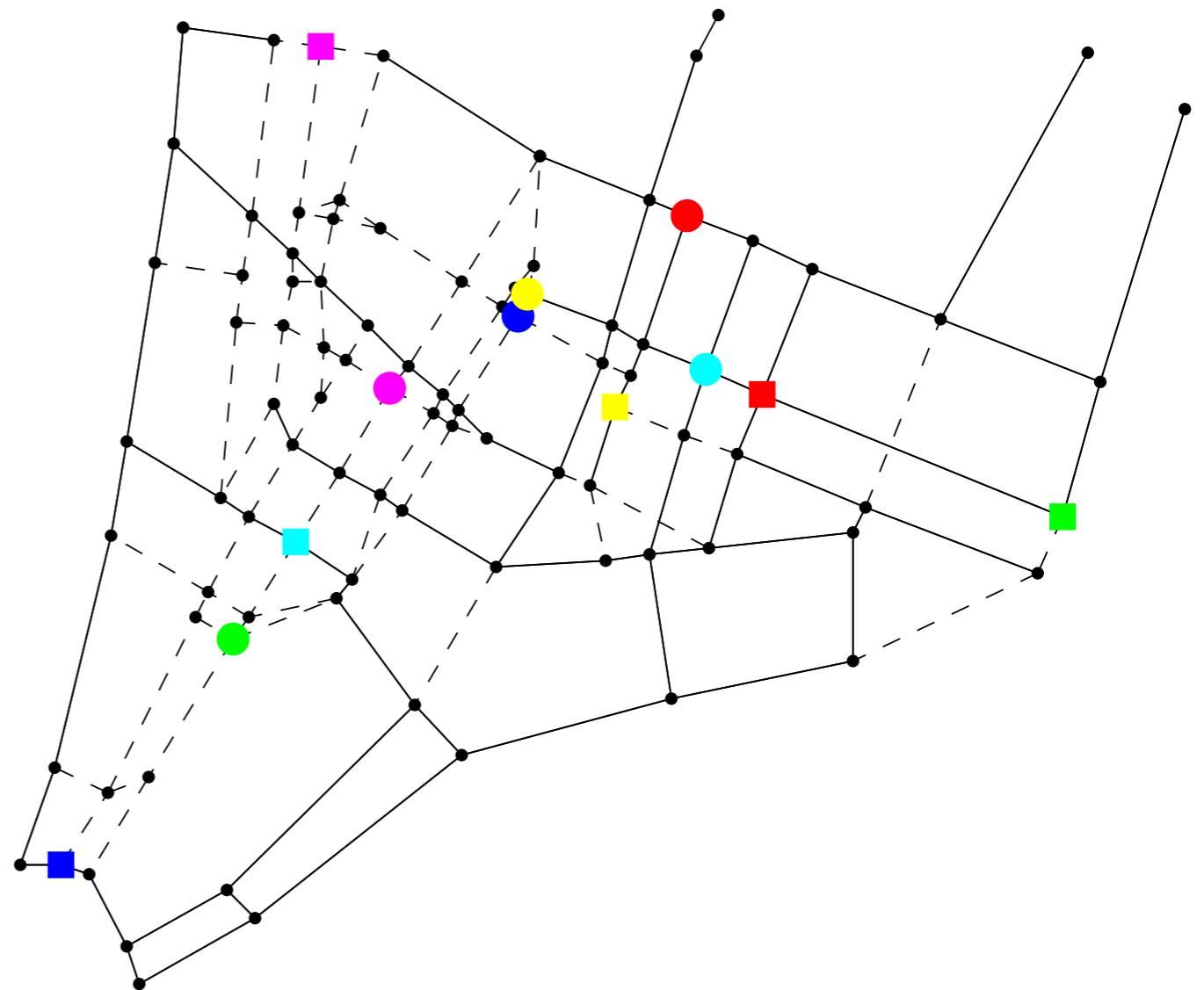


Congestion is a **threshold** phenomenon



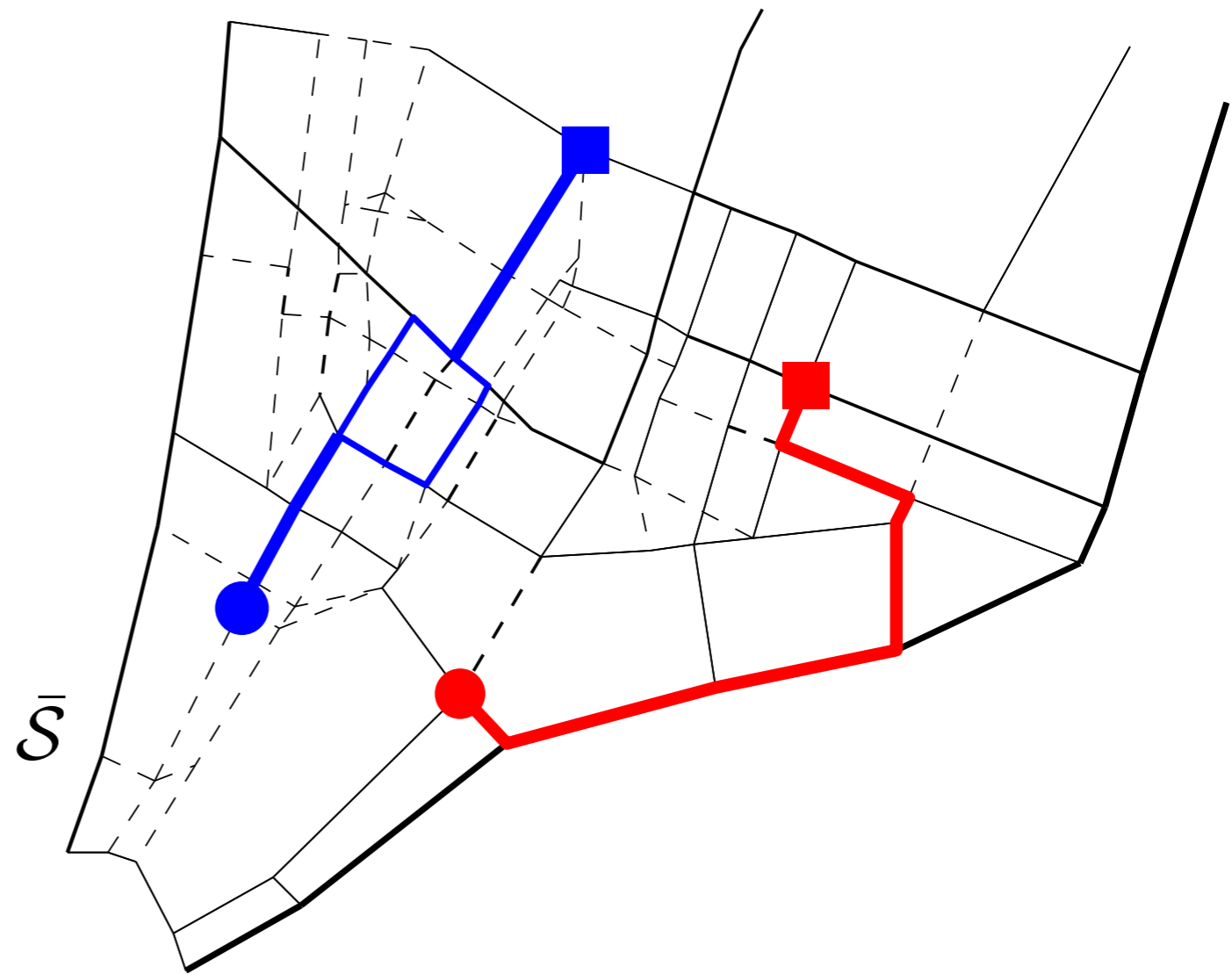
Customers and roads

- Transportation requests: origin, destination, rate of demand (customers/minute)
- Trips:
 - Customer trips service transportation requests
 - Rebalancing trips realign vehicles with requests
- Road network model:
 - Nodes: intersections
 - Directed, capacitated edges: roads



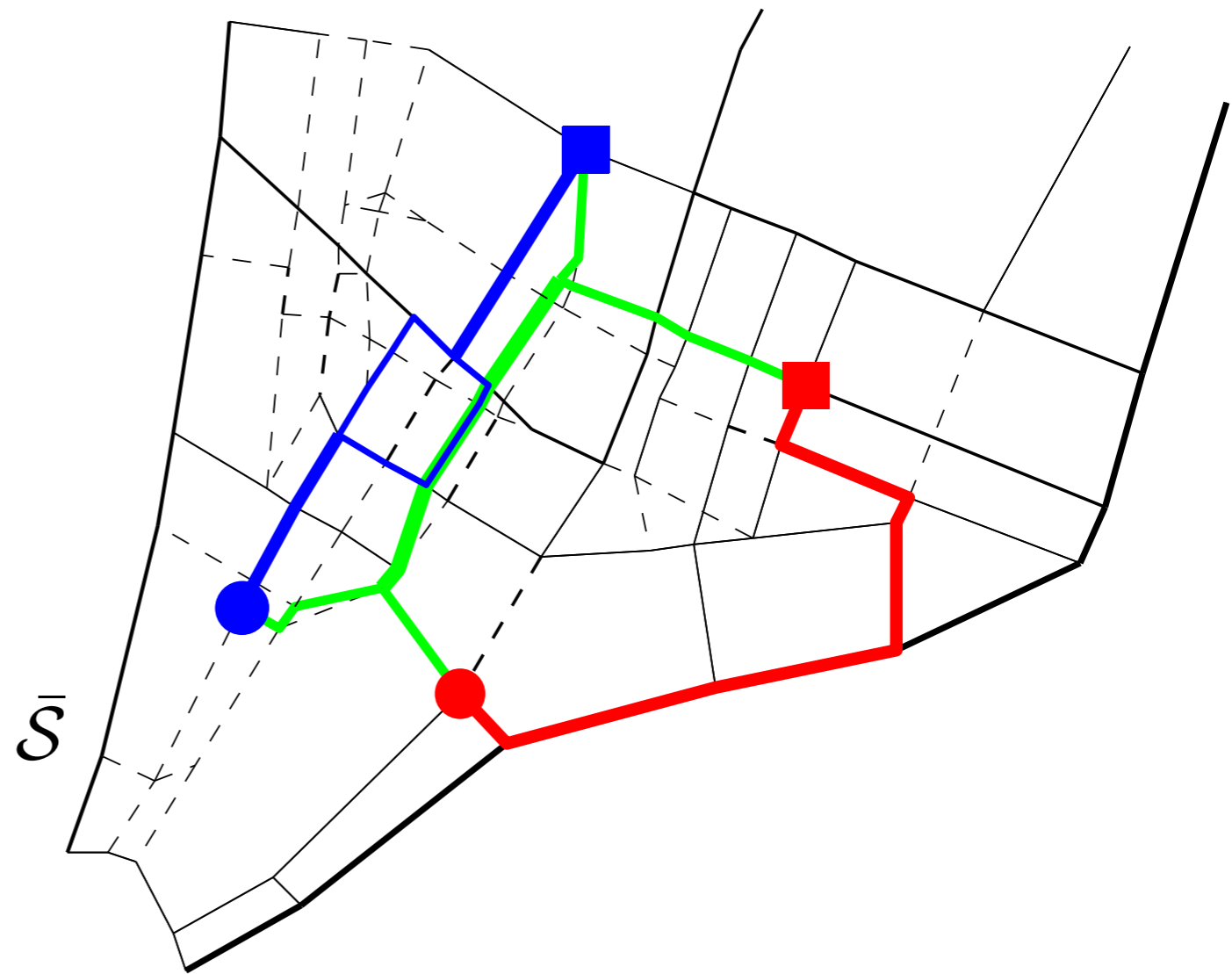
Road network and flows

- Customer flows
- Rebalancing flows
- Graph cut $(\mathcal{S}, \bar{\mathcal{S}})$
 - ▶ Edges separating \mathcal{S} and $\bar{\mathcal{S}}$
 - ▶ Cut capacity $C_{\text{out}}, C_{\text{in}}$



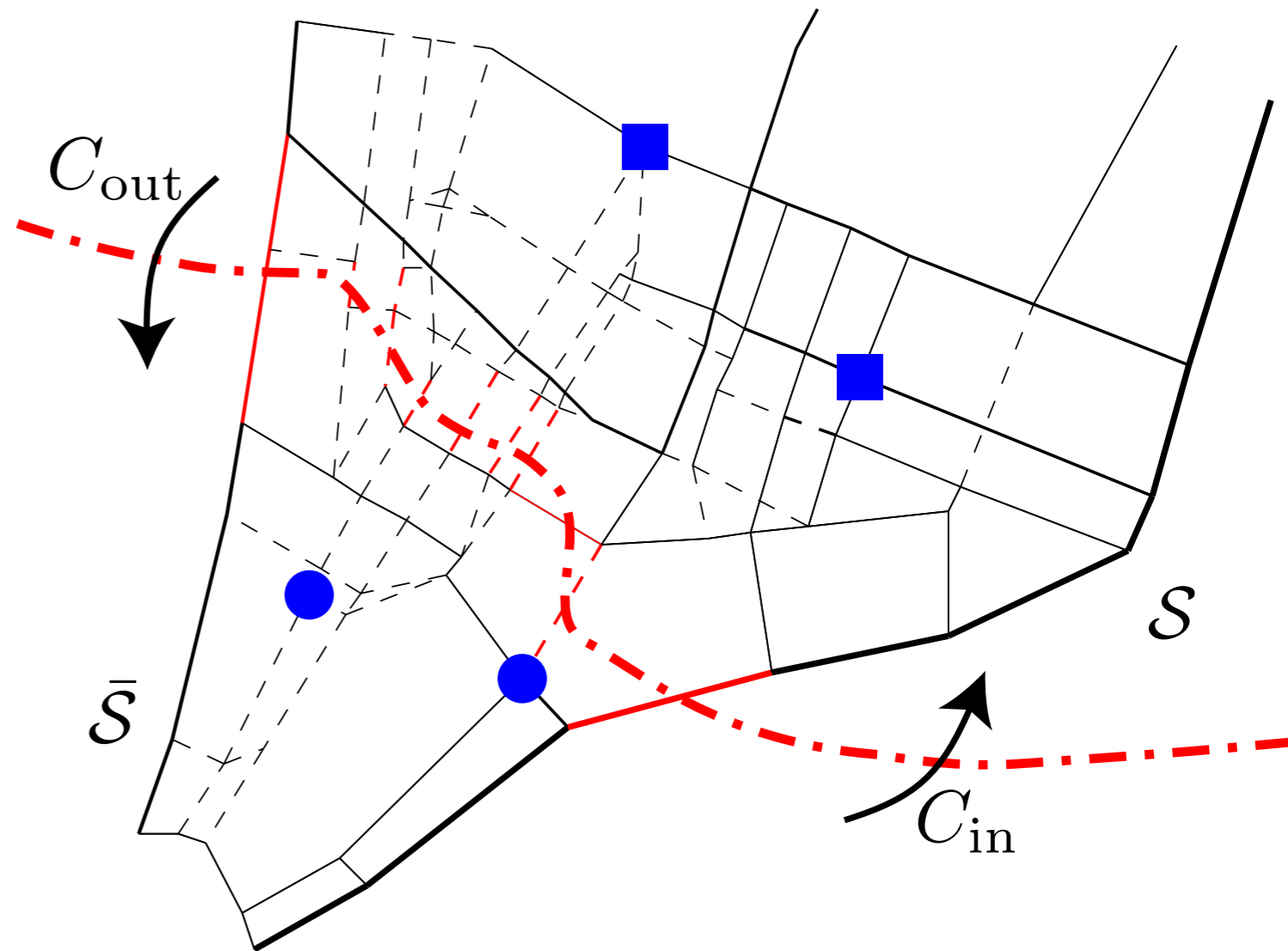
Road network and flows

- Customer flows
- Rebalancing flows
- Graph cut $(\mathcal{S}, \bar{\mathcal{S}})$
 - ▶ Edges separating \mathcal{S} and $\bar{\mathcal{S}}$
 - ▶ Cut capacity $C_{\text{out}}, C_{\text{in}}$



Road network and flows

- Customer flows
- Rebalancing flows
- Graph cut $(\mathcal{S}, \bar{\mathcal{S}})$
 - ▶ Edges separating \mathcal{S} and $\bar{\mathcal{S}}$
 - ▶ Cut capacity $C_{\text{out}}, C_{\text{in}}$



Linear model

minimize
 $f_m(\cdot, \cdot), f_R(\cdot, \cdot)$

$$\sum_{m \in \mathcal{M}} \sum_{(u,v) \in \mathcal{E}} t(u,v) f_m(u,v) + \rho \sum_{(u,v) \in \mathcal{E}} t(u,v) f_R(u,v)$$

subject to

$$\sum_{u \in \mathcal{V}} f_m(u, s_m) + \lambda_m = \sum_{w \in \mathcal{V}} f_m(s_m, w) \quad \forall m \in \mathcal{M}$$

$$\sum_{u \in \mathcal{V}} f_m(u, t_m) = \lambda_m + \sum_{w \in \mathcal{V}} f_m(t_m, w) \quad \forall m \in \mathcal{M}$$

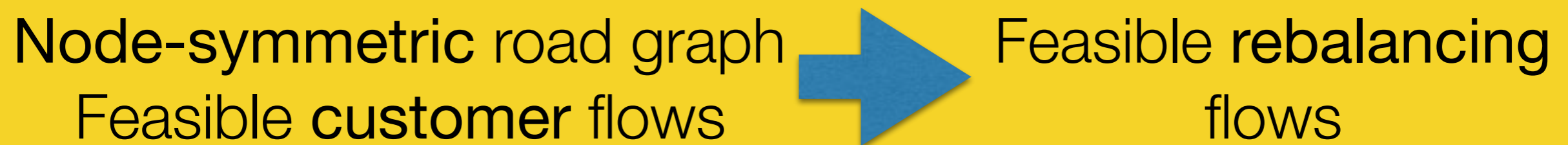
$$\sum_{u \in \mathcal{V}} f_m(u, v) = \sum_{w \in \mathcal{V}} f_m(v, w) \quad \forall m \in \mathcal{M}, v \in \mathcal{V} \setminus \{s_m, t_m\}$$

$$\sum_{u \in \mathcal{V}} f_R(u, v) + \sum_{m \in \mathcal{M}} 1_{v=t_m} \lambda_m = \sum_{w \in \mathcal{V}} f_R(v, w) + \sum_{m \in \mathcal{M}} 1_{v=s_m} \lambda_m \quad \forall v \in \mathcal{V}$$

$$f_R(u, v) + \sum_{m \in \mathcal{M}} f_m(u, v) \leq c(u, v) \quad \forall (u, v) \in \mathcal{E}$$

Theoretical results

Sufficient condition for feasibility of rebalancing



1. In a node-symmetric road network **rebalancing does not increase congestion**
2. If goal is to maximize customer satisfaction, customer flows and rebalancing flows are **decoupled** and can be computed separately

Are road networks symmetric?

Urban center	Avg. frac. capacity disparity	Std. dev.
Chicago, IL	$1.2972 \cdot 10^{-4}$	$1.003 \cdot 10^{-4}$
New York, NY	$1.6556 \cdot 10^{-4}$	$1.304 \cdot 10^{-4}$
Colorado Springs, CO	$3.1772 \cdot 10^{-4}$	$2.308 \cdot 10^{-4}$
Los Angeles, CA	$0.9233 \cdot 10^{-4}$	$0.676 \cdot 10^{-4}$
Mobile, AL	$1.9368 \cdot 10^{-4}$	$1.452 \cdot 10^{-4}$
Portland, OR	$1.0769 \cdot 10^{-4}$	$0.778 \cdot 10^{-4}$

Very high degree of node-symmetry
(even with many one-way streets)

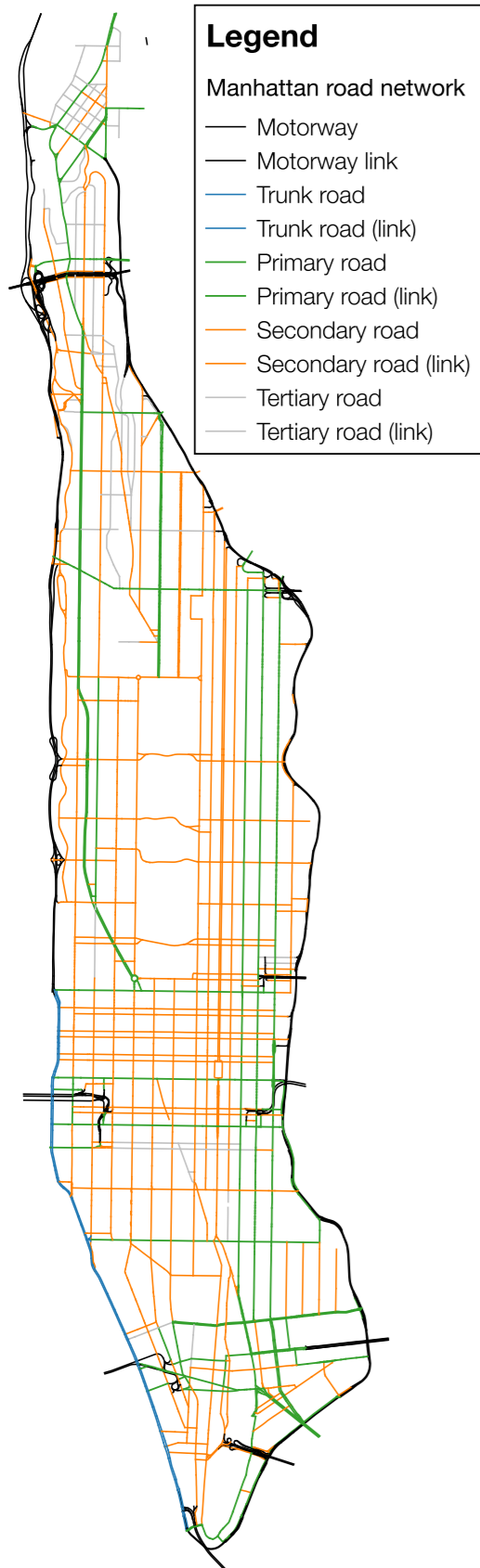


A real-time congestion-aware rebalancing algorithm

- Customers are routed on **fastest route** as soon as a vehicle is available
- Empty vehicles are rebalanced by a **batch algorithm**
 - ▶ Tries to match a given vehicle distribution
 - ▶ Minimum-cost **congestion-free** rebalancing flows
 - ▶ Computationally efficient (**totally unimodular**)

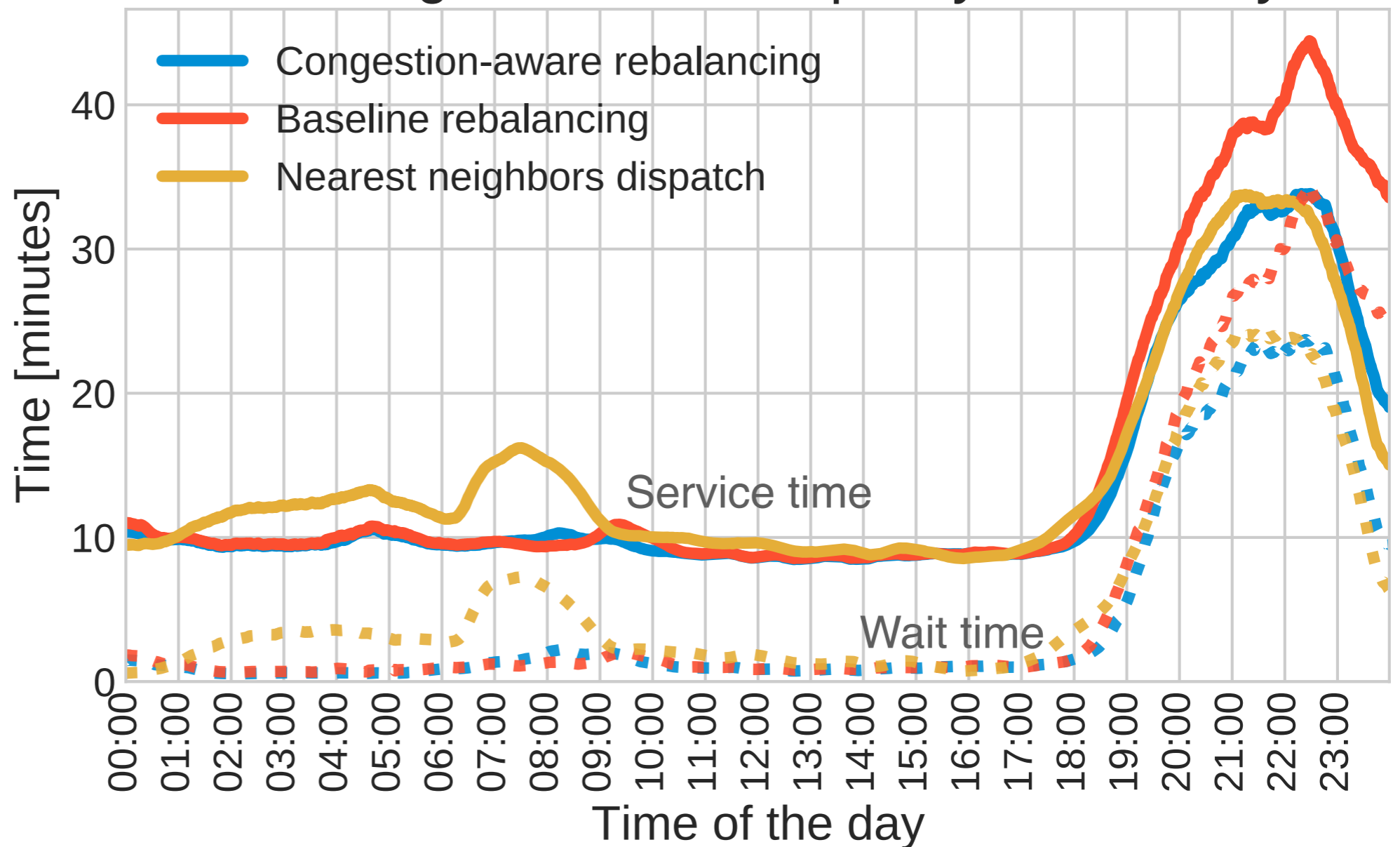
$$\begin{aligned}
 & \underset{f_R(\cdot, \cdot), \{ds_i\}, \{dt_j\}}{\text{minimize}} && \sum_{(u,v) \in \mathcal{E}} t(u,v) f_R(u,v) + \sum_{i \in S_R} C ds_i + \sum_{i \in T_R} C dt_i \\
 & \text{subject to} && \sum_{u \in \mathcal{V}} f_R(u,v) + 1_{v \in S_R} (v_v^e(t) - v_v^d(t) - ds_v) \\
 & && = \sum_{w \in \mathcal{V}} f_R(v,w) + 1_{v \in T_R} (v_v^d(t) - v_v^e(t) - dt_v), \\
 & && \forall v \in \mathcal{V} \\
 & && f_R(u,v) \leq c_R(u,v), \quad \forall (u,v) \in \mathcal{E}, \\
 & && f_R(u,v) \geq 0, \quad \forall (u,v) \in \mathcal{E}, \\
 & && ds_i, dt_j \geq 0, \quad \forall i \in S_R, j \in T_R.
 \end{aligned}$$

Case study: NYC



- 24-hour simulation
- NYC taxi data: 480000 customers
- 8000 vehicles

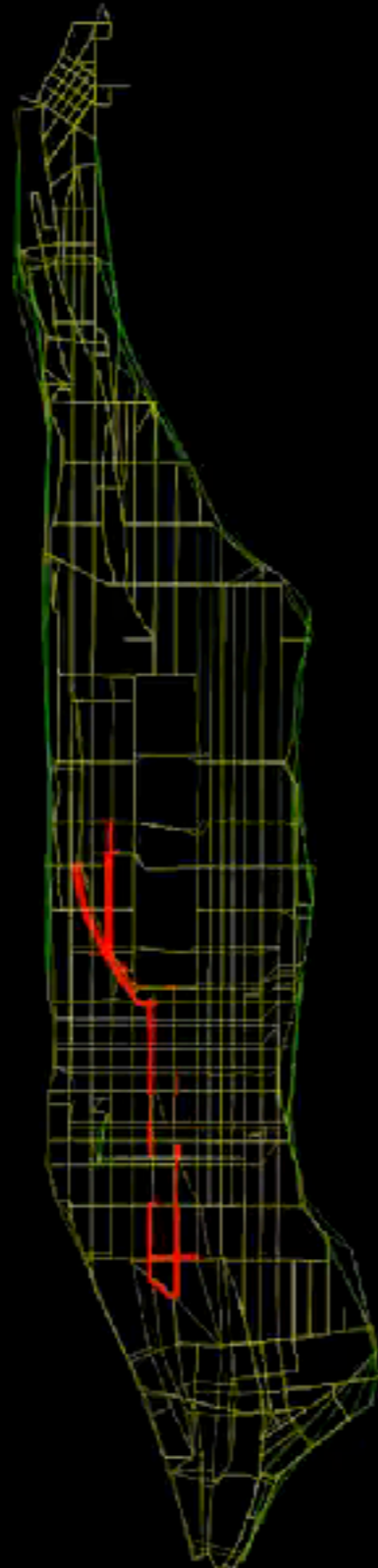
Medium congestion: road capacity reduced by 75%



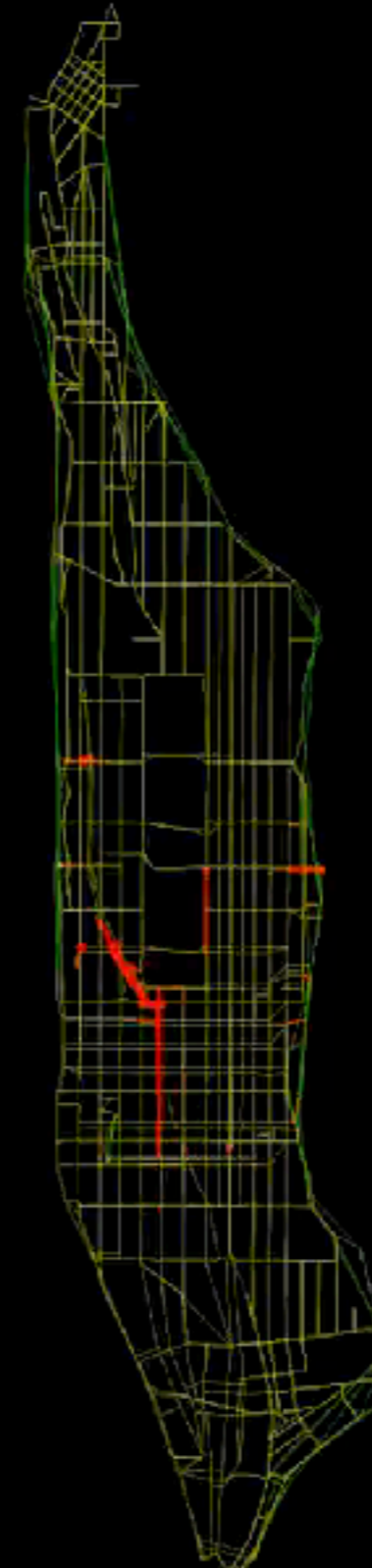
Experimental results



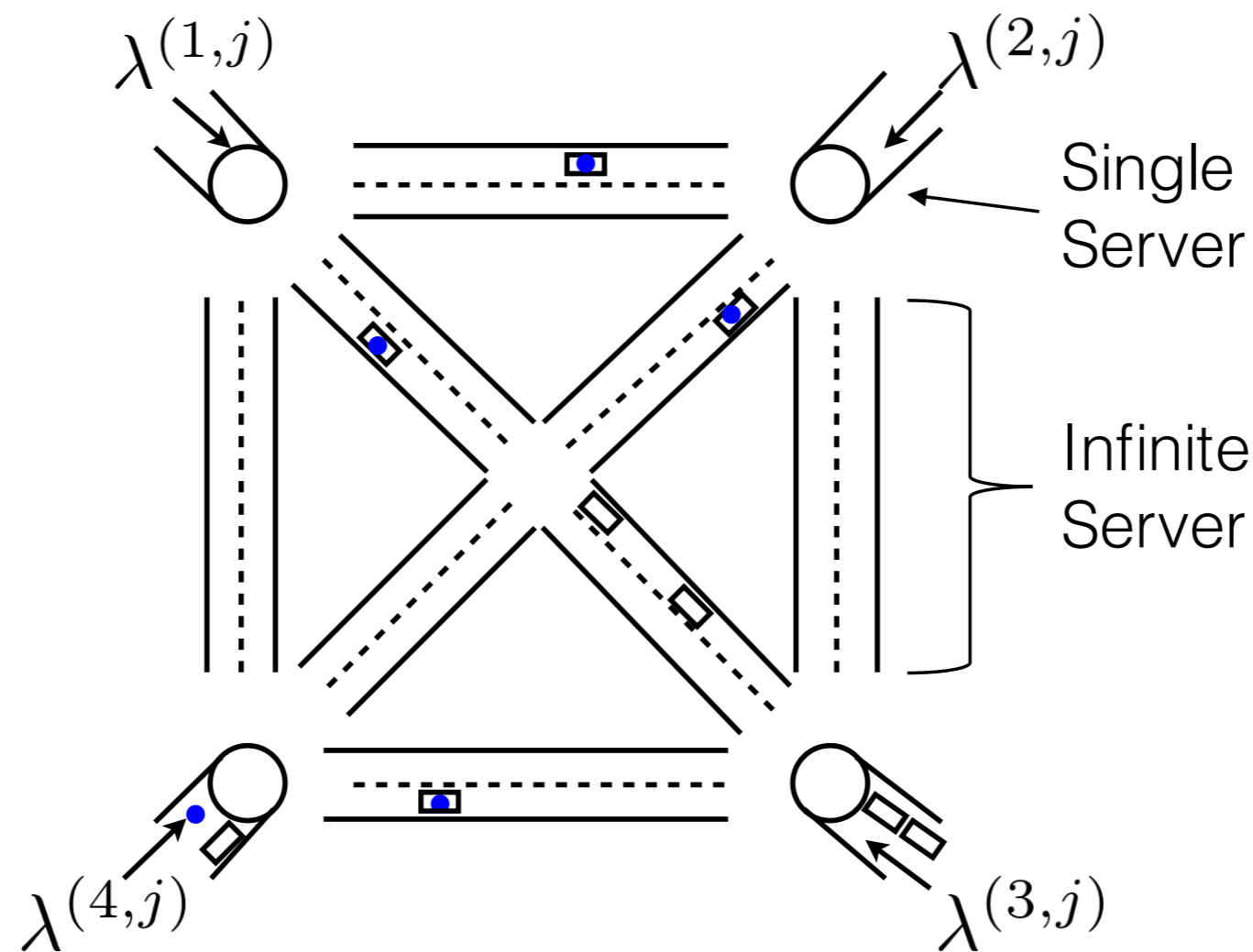
Baseline



Congestion aware



A BCMP queuing network model for congested AMoD systems



Network flow model is **equivalent** to a queuing-theoretical model for systems with **high availability**

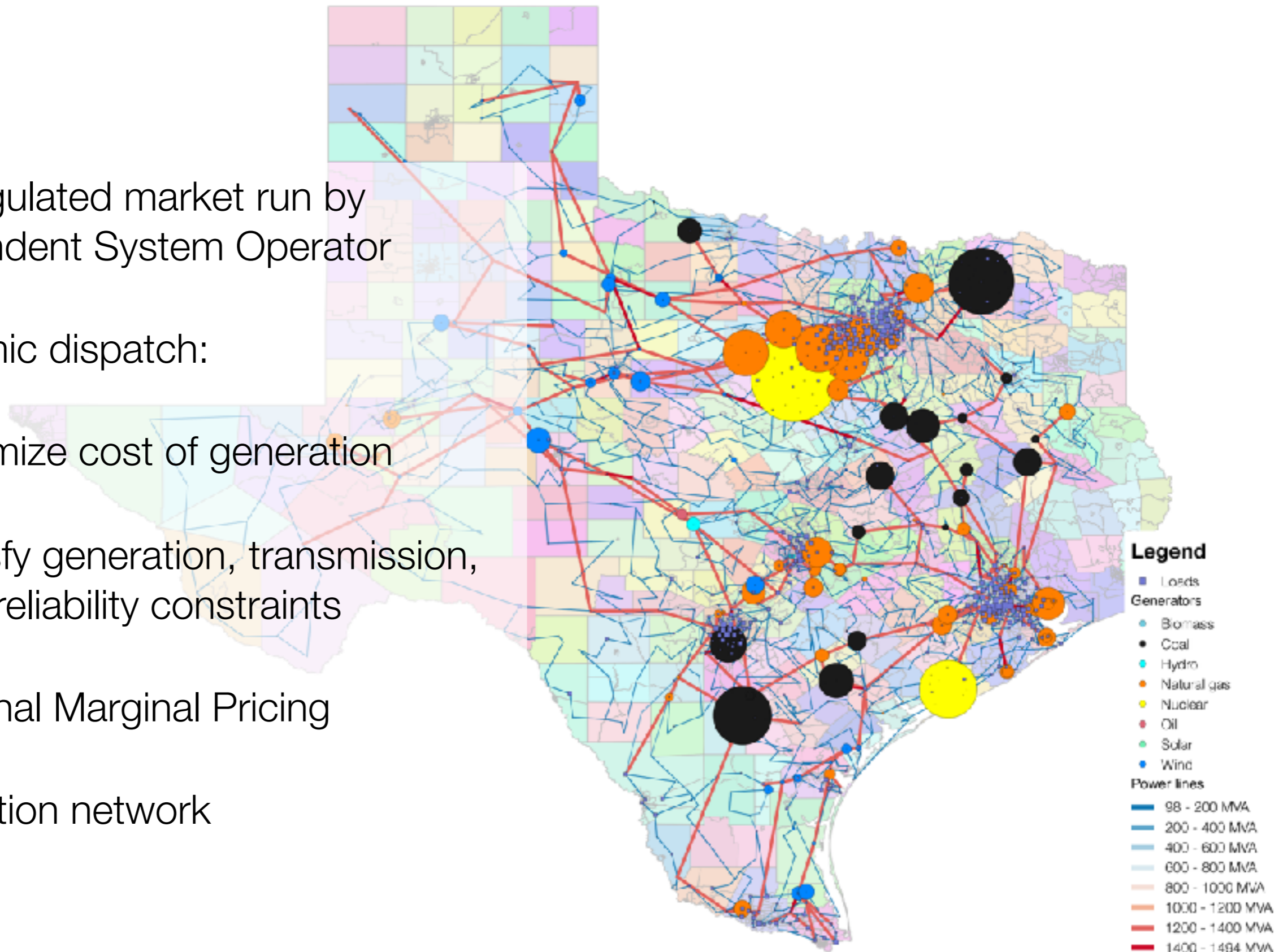


PART II

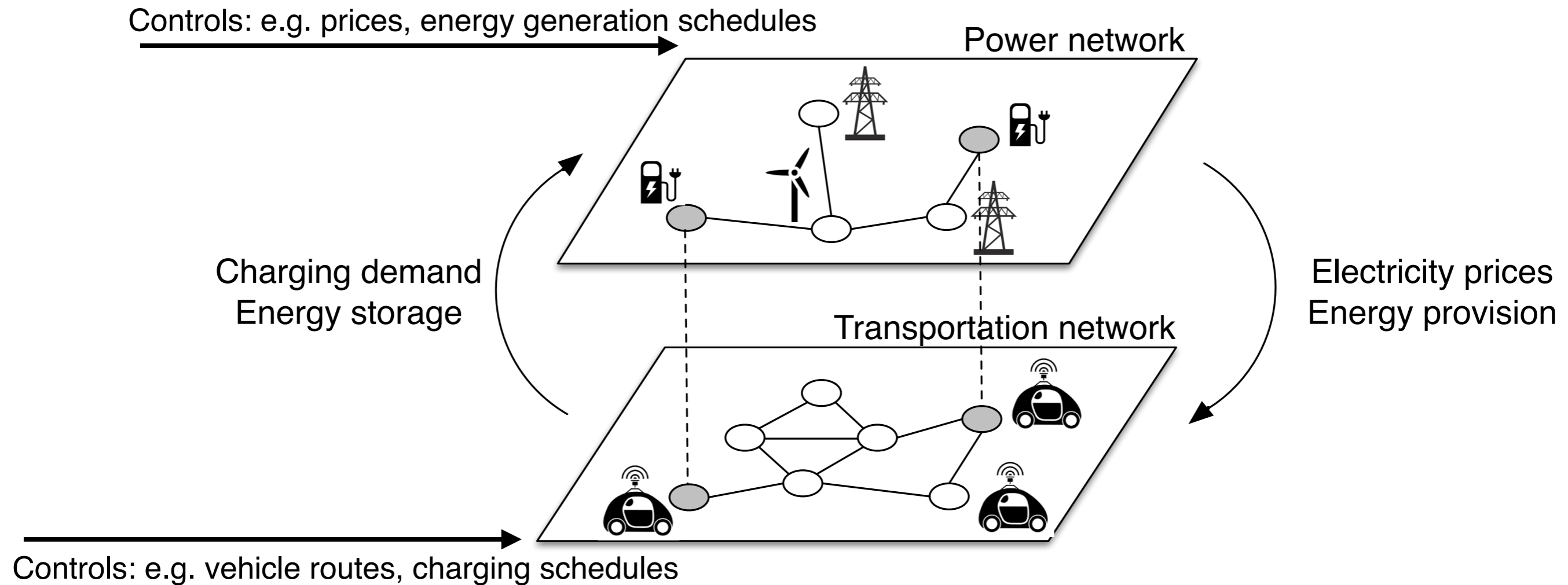
AMoD SYSTEMS AND THE POWER NETWORK

The electric power network

- Well-regulated market run by Independent System Operator
- Economic dispatch:
 - Minimize cost of generation
 - Satisfy generation, transmission, and reliability constraints
- Locational Marginal Pricing
- Distribution network



AMoD and the power network

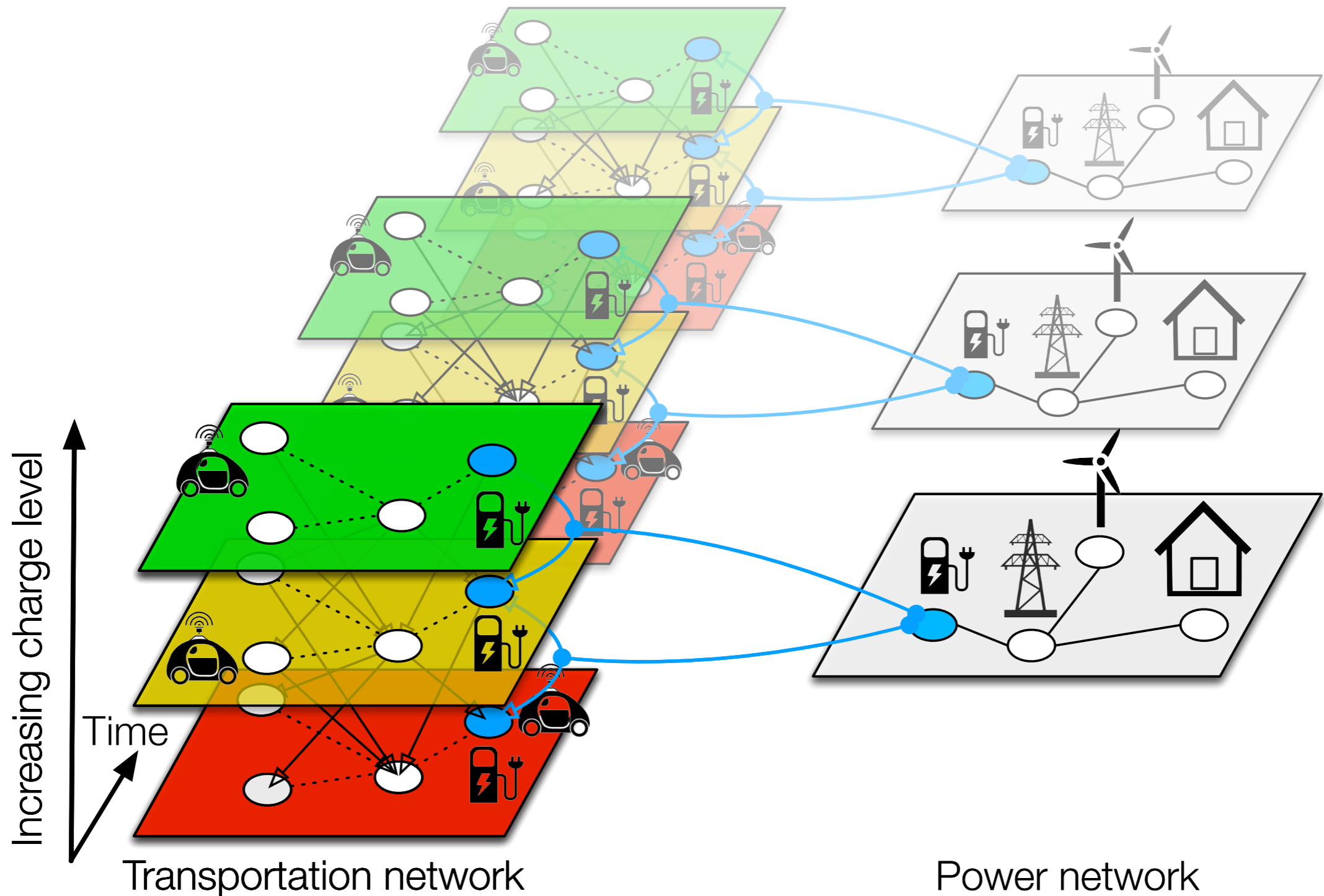


Goal: **socially optimal** control policy for the AMoD system and the power network

Assumptions

- **Cooperation** between the transportation system operator and the power network's independent system operator
- Road network: **network flow** model
- Power transmission network: **DC** model
- Power distribution network: **thermal** constraints only
- Transportation system buys/sells electricity at **LMP** rate

Augmented AMoD network flow model



Linear model

$$\underset{f_m, \lambda_m^{c,\text{in}}, \lambda_m^{c,t,\text{out}}, N_F, \theta, p}{\text{minimize}} \quad V_T \left(\sum_{(\mathbf{v}, \mathbf{w}) \in \mathcal{E}} t_{\mathbf{v}, \mathbf{w}} \sum_{m=1}^M f_m(\mathbf{v}, \mathbf{w}) \right) + V_D \left(\sum_{(\mathbf{v}, \mathbf{w}) \in \mathcal{E}} d_{v_{\mathbf{v}}, v_{\mathbf{w}}} \sum_{m=0}^M f_m(\mathbf{v}, \mathbf{w}) \right) + \sum_{t=1}^T \sum_{g \in \mathcal{G}} o_g(t) p(g, t)$$

subject to

$$\sum_{\mathbf{u}: (\mathbf{u}, \mathbf{v}) \in \mathcal{E}} f_m(\mathbf{u}, \mathbf{v}) + 1_{v_{\mathbf{v}}=v_m} 1_{t_{\mathbf{v}}=t_m} \lambda_m^{c_{\mathbf{v}}, \text{in}} = \sum_{\mathbf{w}: (\mathbf{v}, \mathbf{w}) \in \mathcal{E}} f_m(\mathbf{v}, \mathbf{w}) + 1_{v_{\mathbf{v}}=w_m} \lambda_m^{t_{\mathbf{v}}, c_{\mathbf{v}}, \text{out}}, \quad \forall \mathbf{v} \in \mathcal{V}, m \in \{1, \dots, M\},$$

$$\sum_{c=1}^C \lambda_m^{c,\text{in}} = \lambda_m, \quad \forall m \in \{1, \dots, M\},$$

$$\sum_{t=1}^T \sum_{c=1}^C \lambda_m^{t,c,\text{out}} = \lambda_m, \quad \forall m \in \{1, \dots, M\},$$

$$\sum_{\mathbf{u}: (\mathbf{u}, \mathbf{v}) \in \mathcal{E}} f_0(\mathbf{u}, \mathbf{v}) + \sum_{m=1}^M 1_{v_{\mathbf{v}}=w_m} \lambda_m^{t_{\mathbf{v}}, c_{\mathbf{v}}, \text{out}} + N_I(\mathbf{v}) = \sum_{\mathbf{w}: (\mathbf{v}, \mathbf{w}) \in \mathcal{E}} f_0(\mathbf{v}, \mathbf{w}) + \sum_{m=1}^M 1_{v_{\mathbf{v}}=v_m} 1_{t_{\mathbf{v}}=t_m} \lambda_m^{c_{\mathbf{v}}, \text{in}} + N_F(\mathbf{v}), \quad \forall \mathbf{v} \in \mathcal{V},$$

$$\sum_{c_{\mathbf{v}}=1}^M \left(\sum_{m=0}^M f_m(\mathbf{v}, \mathbf{w}) \right) \leq \bar{f}_{(v_{\mathbf{v}}, v_{\mathbf{w}})}, \quad \forall (v_{\mathbf{v}}, v_{\mathbf{w}}) \in \mathcal{E}_R, \forall t_{\mathbf{v}} \in \{1, \dots, T\},$$

$$\sum_{\substack{(v, w) \in \mathcal{E}_S: \\ v_{\mathbf{v}}=v_{\mathbf{w}}=s, \\ t_{\mathbf{v}} \leq t < t_{\mathbf{w}}}} \left(\sum_{m=0}^M f_m(\mathbf{v}, \mathbf{w}) \right) \leq \bar{S}_s, \quad \forall s \in \mathcal{S}, t \in \{1, \dots, T\},$$

$$\sum_{(u, v) \in \mathcal{E}_P} \frac{\theta(u, t) - \theta(v, t)}{x_{u, v}} + 1_{v \in \mathcal{G}} p(v, t) = 1_{v \in \mathcal{L}} d_v(t) + \sum_{(v, w) \in \mathcal{E}_P} \frac{\theta(v, t) - \theta(w, t)}{x_{v, w}}, \quad \forall v \in \mathcal{B}, t \in \{1, \dots, T\},$$

$$-\bar{p}_{b_1, b_2} \leq \frac{\theta(b_1, t) - \theta(b_2, t)}{x_{b_1, b_2}} \leq \bar{p}_{b_1, b_2}, \quad \forall (b_1, b_2) \in \mathcal{E}_P, t \in \{1, \dots, T\},$$

$$\underline{p}_g(t) \leq p(g, t) \leq \bar{p}_g(t), \quad \forall g \in \mathcal{G}, t \in \{1, \dots, T\},$$

$$-p_g^-(t) \leq p(g, t+1) - p(g, t) \leq p_g^+(t), \quad \forall g \in \mathcal{G}, t \in \{1, \dots, T-1\},$$

$$d_l(t) \leq \bar{d}_l(t), \quad \forall l \in \mathcal{L}, t \in \{1, \dots, T\},$$

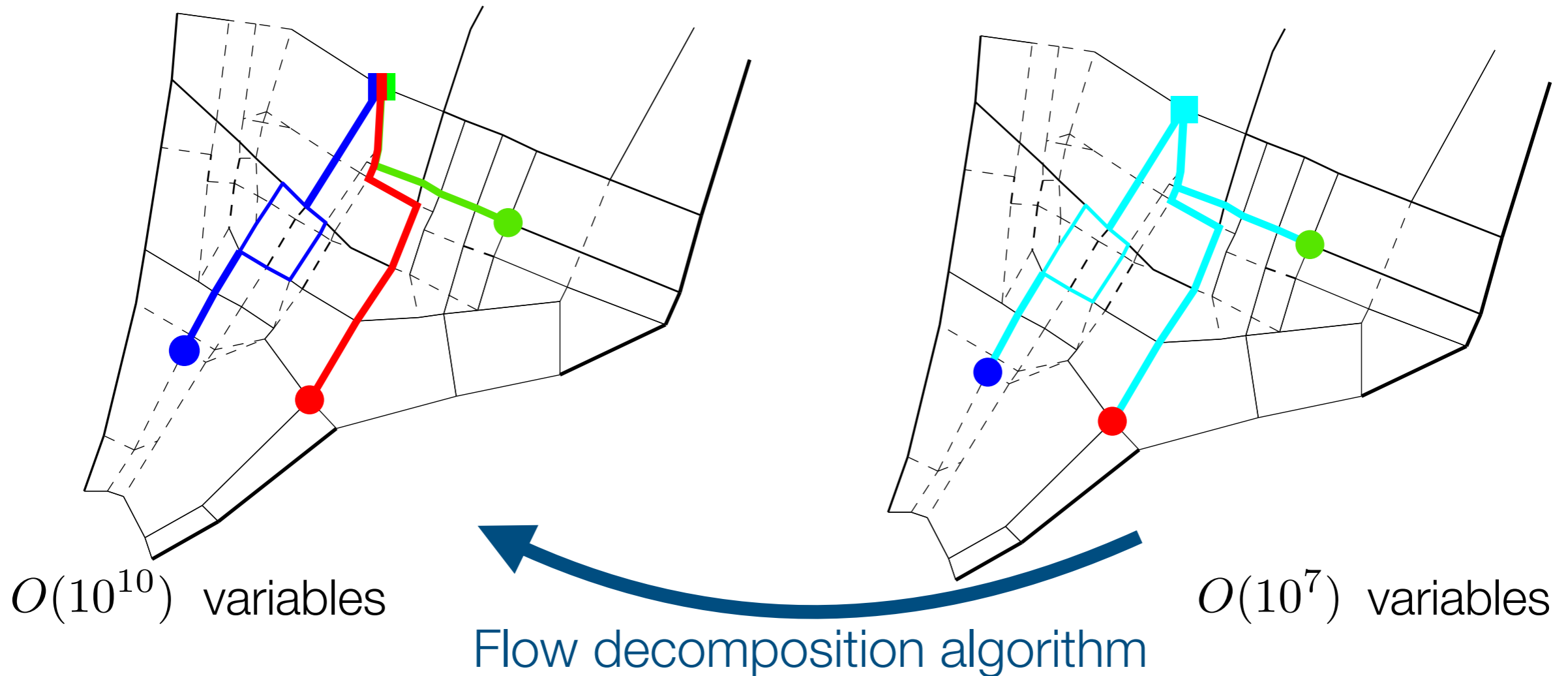
$$d_l(t) = d_{l,e}(t) + J_C \delta c_{M_{P,R}(l)}^+ \sum_{(\mathbf{v}, \mathbf{w}) \in M_{P,G}^+(l,t)} \sum_{m=0}^M f_m(\mathbf{v}, \mathbf{w}) + J_C \delta c_{M_{P,R}(l)}^- \sum_{(\mathbf{v}, \mathbf{w}) \in M_{P,G}^-(l,t)} \sum_{m=1}^M f_m(\mathbf{v}, \mathbf{w}), \quad \forall l \in \mathcal{L}, t \in \{1, \dots, T\}.$$

Flow bundling

Bundle flows with same destination

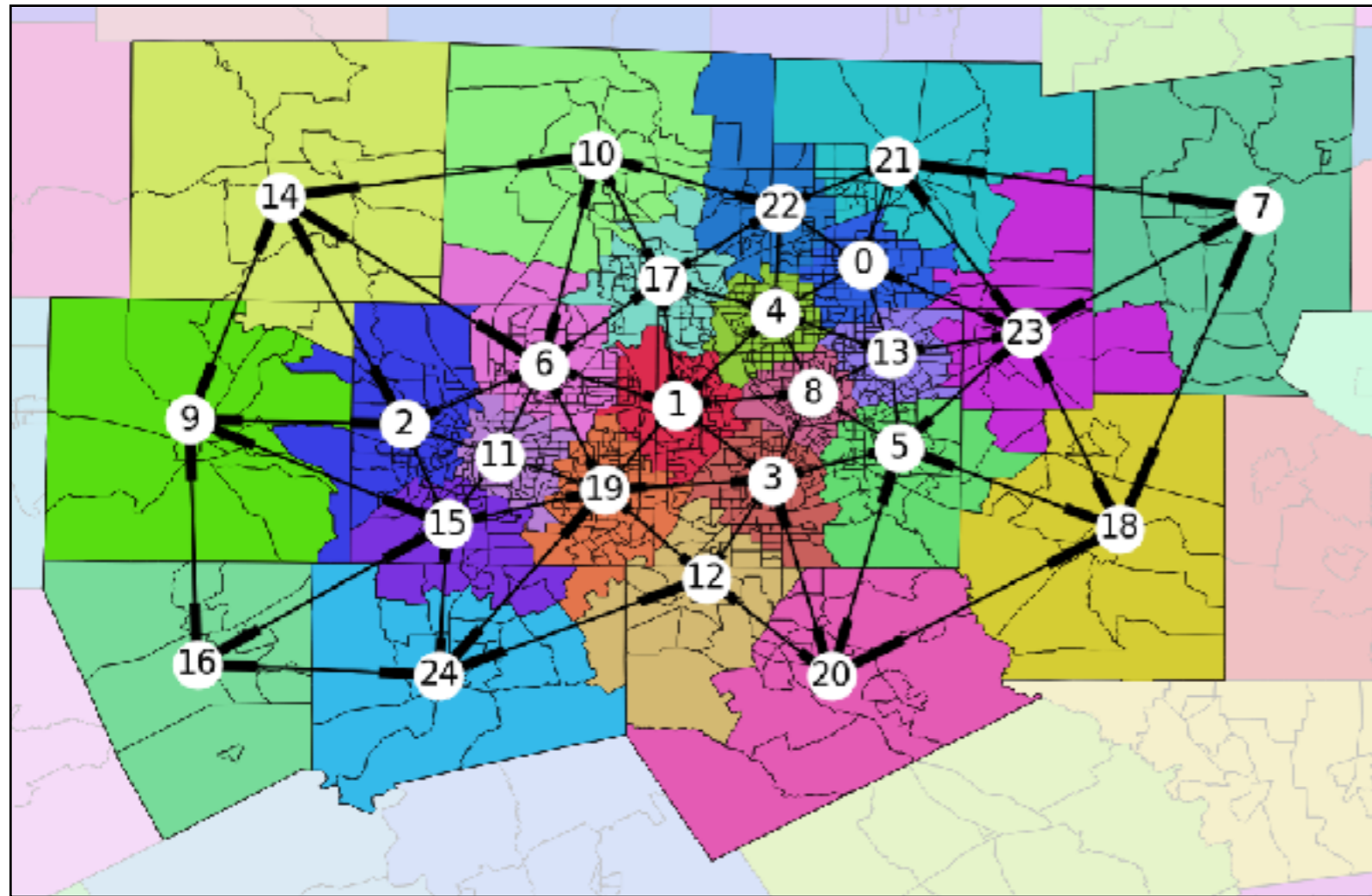
$$O(|\mathcal{V}_R|^2 T (|\mathcal{E}_R| + |\mathcal{S}|) CT)$$

$$O(|\mathcal{V}_R| (|\mathcal{E}_R| + |\mathcal{S}|) CT)$$

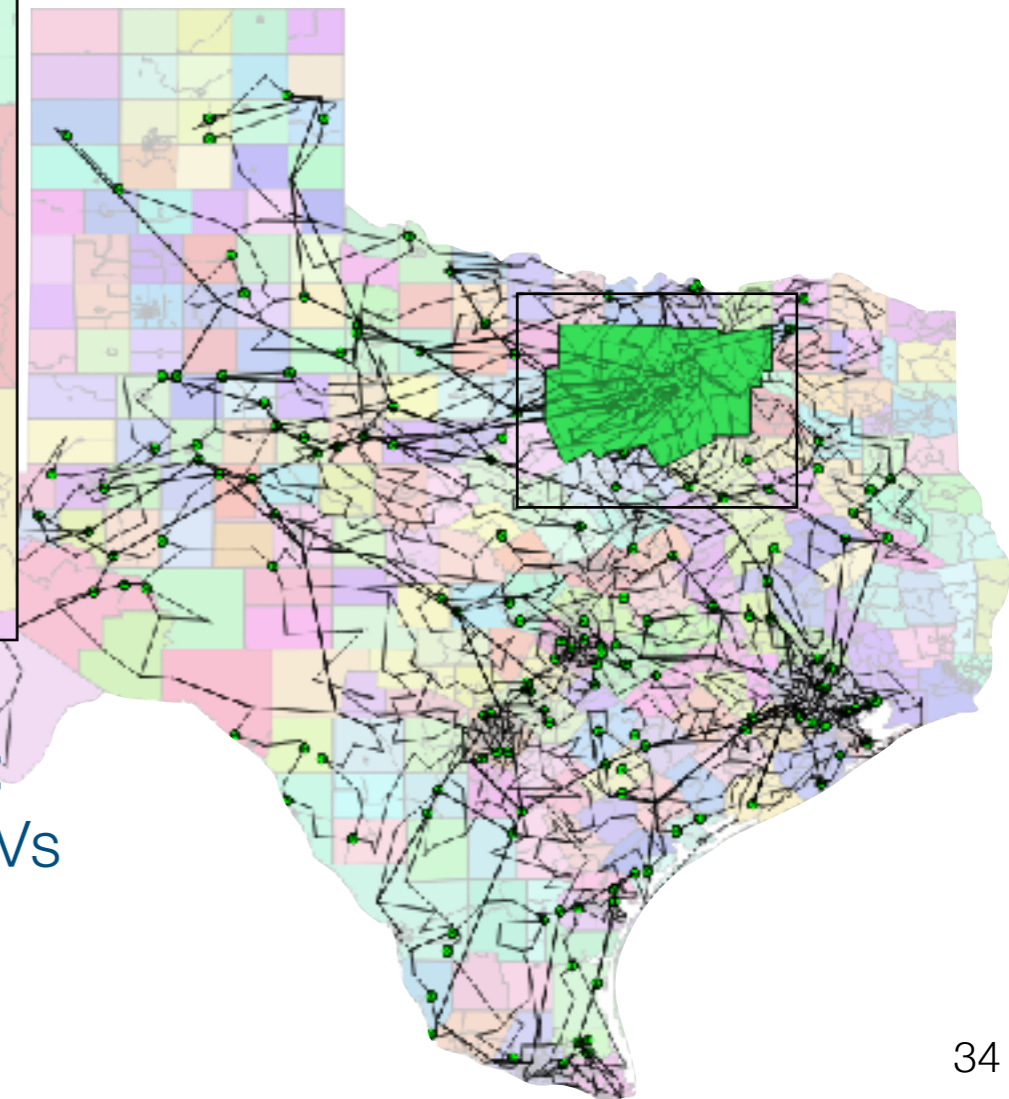


Theorem: flow bundling is lossless

Case study: Dallas-Fort Worth



Power network
282 generators
2007 buses
2481 transmission lines



Road network

25 nodes
173 road links
30 charge levels

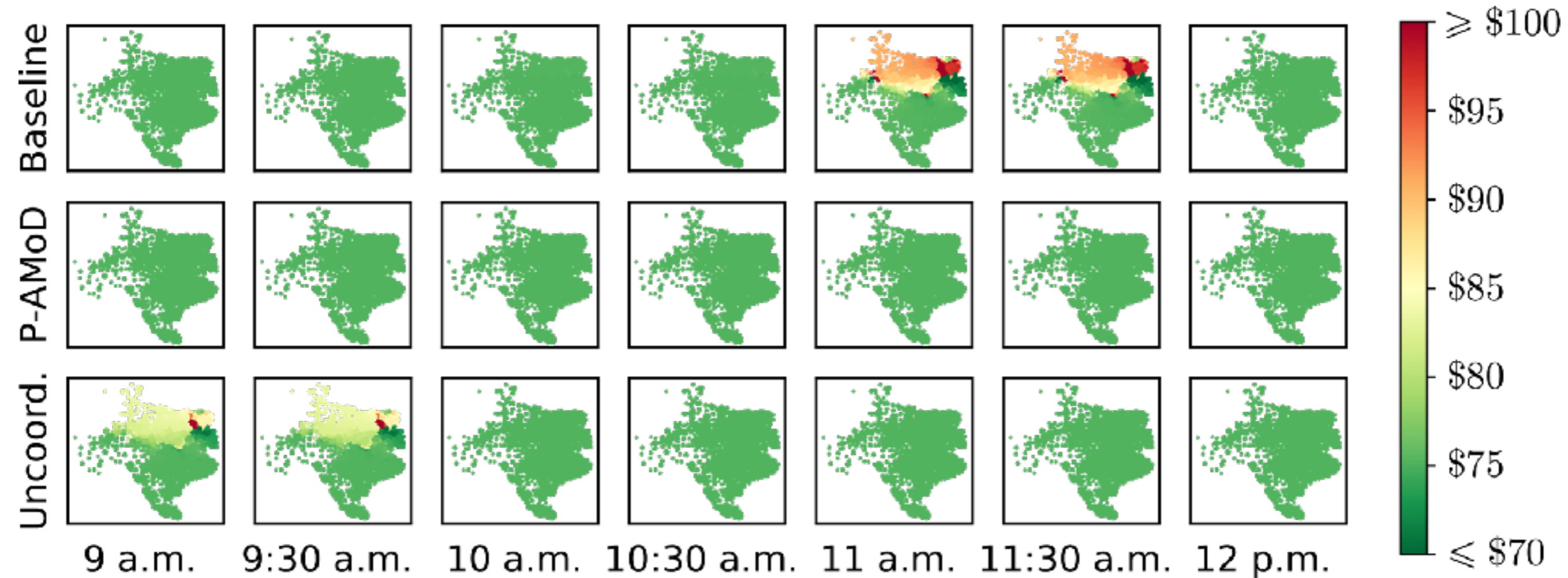
Trips

10 hours
6250 O-D-T pairs
400,000 customers

EV fleet

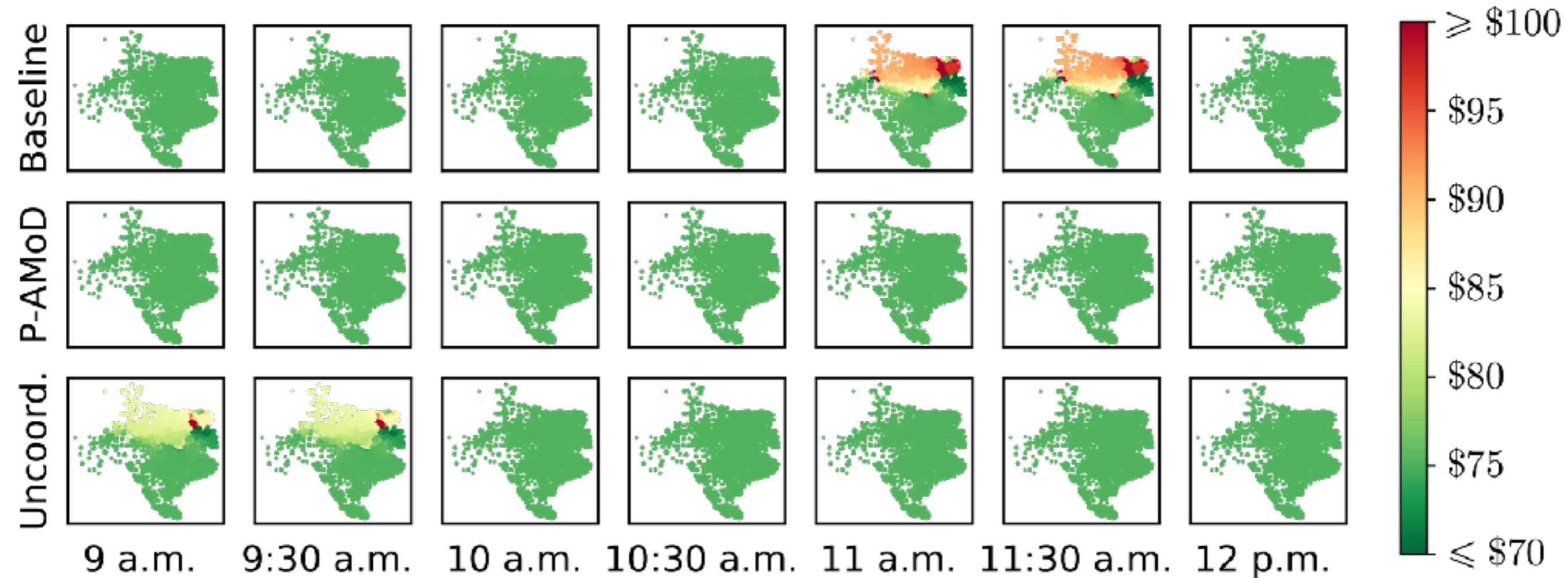
150,000 EVs

Experimental results



	No cars	P-AMoD	Uncoordinated
Avg. passenger travel time	-	1h15m11s	1h15m11s
Tot. energy demand [GWh]	517.498	520.541	520.979
Tot. electricity expenditure [k\$]	39,604.71	39,264.84	39,629.50
w.r.t. no cars [k\$]	-	-339.87	+24.79
Avg. power price in DFW [\$/MWh]	78.68	75.79	77.47
TSO tot. elec. expenditure [k\$]	-	227.98	296.82

Experimental results



Coordination **does not affect** passenger **travel times**

Coordination **reduces** the total price of electricity w.r.t. baseline, despite extra demand!

TSO: **23.5% lower** electricity bill (**\$35M/year**)

Local power network customers: **2.2% lower** electricity bill (**\$122M/year**)

Self-interested actors

Why would a **self-interested** transportation system operator (TSO) optimize for **social welfare**?

Theorem: the social optimum is a Nash equilibrium

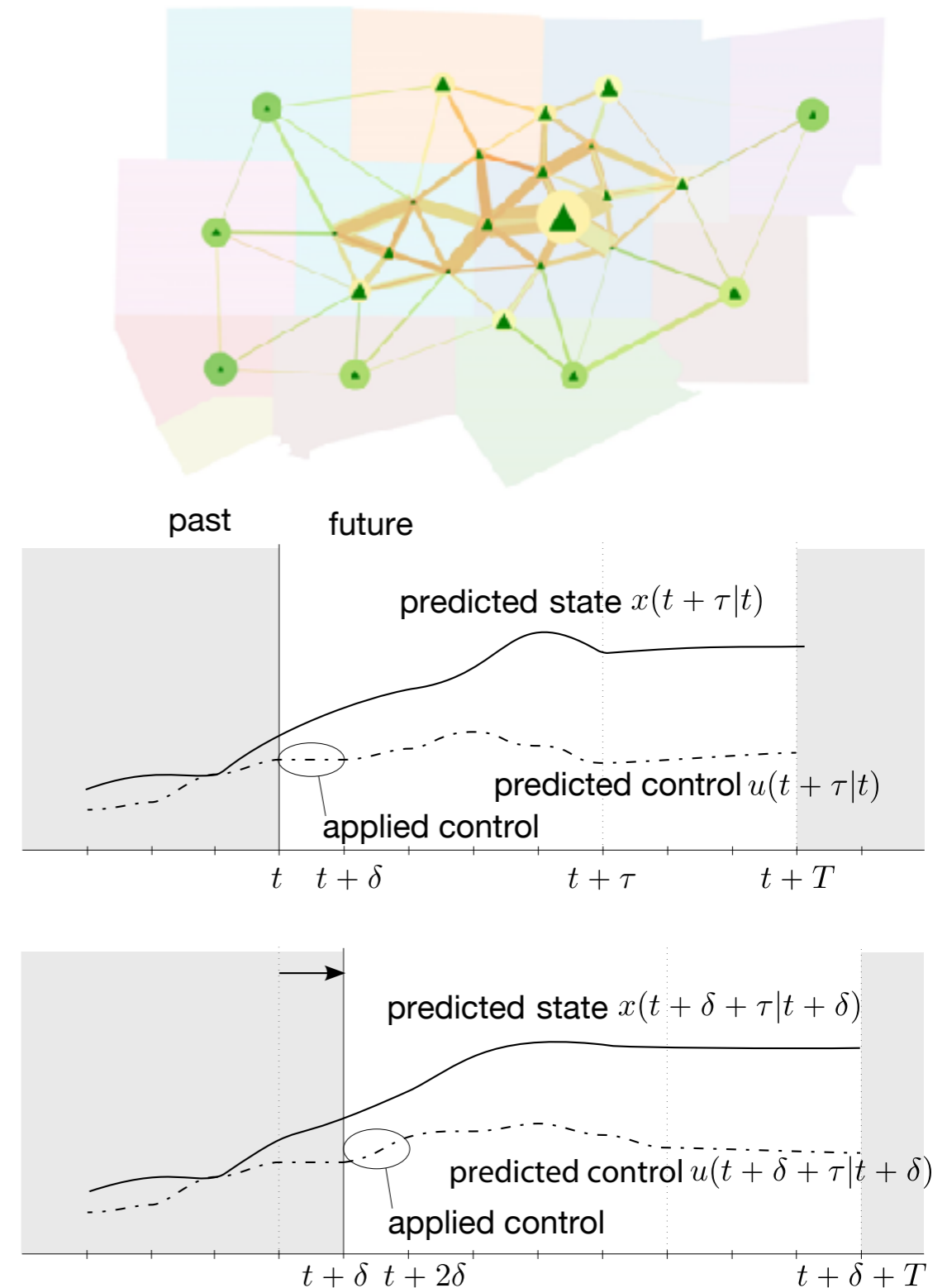
For TSO, optimal charging schedule is the **best response** to given electricity prices (and vice versa).

Theorem: the equilibrium can be computed without sharing private information

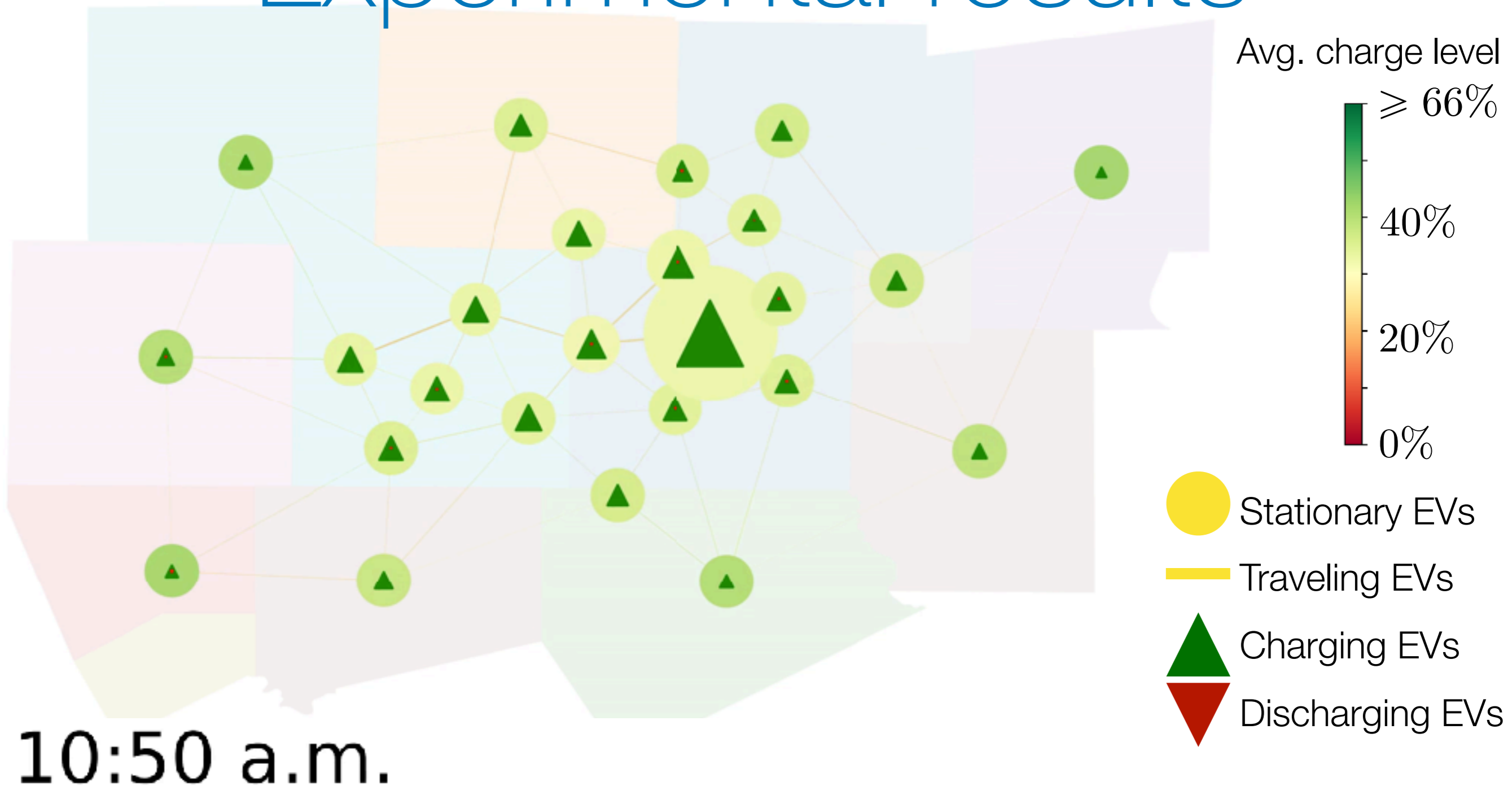
TSO and ISO can compute the optimum with a **dual decomposition** algorithm. Only **public information** (price of electricity and charging schedule) is shared.

A real-time P-AMoD algorithm

- **Assumption:** customer-carrying vehicles always follow **shortest route; no charging** when customers on board
- **Suboptimal**, but **fast** (1h \rightarrow 1m)
- **Receding-horizon** implementation
- Fractional output is **sampled**



Experimental results



TSO: **13.9% lower** electricity bill (**\$16M/year**)

Total electricity expenditure **reduced** by **75M/year** w.r.t. greedy

Local power network customers: **0.88% lower** electricity bill

Conclusions

AMoD systems do not increase congestion if properly routed

- Capacitated network flow model with theoretical guarantees
- Model-predictive control algorithm
- 22% reduction in customer wait times compared to baseline algorithm (NYC)

AMoD systems can act as mobile storage units in the power network

- Joint model for AMoD systems and power network
- Control algorithm: efficient *socially optimal* solution with bundling
- Socially optimal solution is a Nash equilibrium, can be computed with no private information
- Cooperation reduces in 23% lower electricity price for TSO, \$120M in savings for power network customers (DFW)

Future research directions

- Customer demand **prediction**
- **Stochastic control** of AMoD systems
- How should AMoD systems interact with **public transportation**?
- Will AMoD systems foster adoption of **renewable** energy sources?
- What will the effect of AMoD systems on **pollution** be?

Acknowledgements



Acknowledgements





Thanks!

Contact: hello@federico.io



Thanks!

Contact: hello@federico.io



Thanks!

Contact: hello@federico.io

References

- [Ahuja et al., 1993] Ahuja, R. K., Magnanti, T. L., and Orlin, J. B. (1993). *Network Flows: Theory, Algorithms and Applications*. Prentice Hall.
- [Alizadeh et al., 2016] Alizadeh, M., Wai, H.-T., Chowdhury, M., Goldsmith, A., Scaglione, A., and Javidi, T. (2016). Joint management of electric vehicles in coupled power and transportation networks. *IEEE Transactions on Control of Network Systems*. In press.
- [Alizadeh et al., 2014] Alizadeh, M., Wai, H.-T., Scaglione, A., Goldsmith, A., Fan, Y. Y., and Javidi, T. (2014). Optimized path planning for electric vehicle routing and charging. In *Allerton Conf. on Communications, Control and Computing*.
- [Balmer et al., 2009] Balmer, M., Rieser, M., Meister, K., Charypar, D., Lefebvre, N., and Nagel, K. (2009). MATSim-t: Architecture and simulation times. In *Multi-Agent Systems for Traffic and Transportation Engineering*, chapter 3.
- [Barnard, 2016] Barnard, M. (2016). Autonomous cars likely to increase congestion. Available at <http://cleantechnica.com/2016/01/17/autonomous-cars-likely-increase-congestion>.
- [Barth and Todd, 1999] Barth, M. and Todd, M. (1999). Simulation model performance analysis of a multiple station shared vehicle system. *Transportation Research Part C: Emerging Technologies*, 7(4):237-259.
- [Berbeglia et al., 2010] Berbeglia, G., Cordeau, J.-F., and Laporte, G. (2010). Dynamic pickup and delivery problems. *European Journal of Operational Research*, 202(1):8-15.
- [Bertsekas, 1999] Bertsekas, D. (1999). *Nonlinear programming*. Athena Scientific, 2 edition. [Boeing, 2017] Boeing, G. (2017). OSMnx: New methods for acquiring, constructing, analyzing, and visualizing complex street networks. *Computers, Environment and Urban Systems*. Forthcoming. [Bureau of Public Roads, 1964] Bureau of Public Roads (1964). Traffic assignment manual. Technical report, U.S. Department of Commerce, Urban Planning Division.
- [Bureau of Transportation Statistics, 2016] Bureau of Transportation Statistics (2016). National transportation statistics. Technical report, U.S. Department of Transportation.
- [Chevrolet, 2017] Chevrolet (2017). Bolt EV. Available at <http://www.chevrolet.com/bolt-ev-electric-vehicle>.
- [Daganzo, 1994] Daganzo, C. F. (1994). The cell transmission model: A dynamic representation of highway traffic consistent with the hydrodynamic theory. *Transportation Research Part B: Methodological*, 28(4):269-287.
- [Dubhashi and Ranjan, 1996] Dubhashi, D. P. and Ranjan, D. (1996). Balls and bins: A study in negative dependence. *BRICS Report Series*, 3(25):1-27.
- [EIA, 2017] EIA (2017). Levelized cost and levelized avoided cost of new generation resources in the annual energy outlook 2017. Technical report, U.S. Energy Information Administration.
- [Electric Reliability Council of Texas (ERCOT), 2017] Electric Reliability Council of Texas (ERCOT) (2017). Grid information. Available at <http://www.ercot.com/gridinfo/>.
- [Evarts, 2013] Evarts, E. (2013). Many americans are just a plug away from owning an electric car. <https://www.yahoo.com/news/many-americans-just-plug-away-owning-electric-car-160000286.html>.
- [Even et al., 1976] Even, S., Itai, A., and Shamir, A. (1976). On the complexity of timetable and multicommodity flow problems. *SIAM Journal on Computing*, 5(4):691-703.
- [Fagnant and Kockelman, 2014] Fagnant, D. J. and Kockelman, K. M. (2014). The travel and environmental implications of shared autonomous vehicles, using agent-based model scenarios. *Transportation Research Part C: Emerging Technologies*, 40:1-13.
- [Federal Highway Administration, 2014] Federal Highway Administration (2014). Census Transportation Planning Products (CTTP) 2006-2010 Census Tract Flows. Technical report, U.S. Department of Transportation.
- [Ford and Fulkerson, 1962] Ford, L. R. and Fulkerson, D. R. (1962). *Flows in Networks*. Princeton University Press.
- [Glover et al., 2011] Glover, J., Sarma, M., and Overbye, T. (2011). *Power System Analysis and Design*. Cengage Learning, fifth edition.
- [Goeke and Schneider, 2015] Goeke, D. and Schneider, M. (2015). Routing a mixed fleet of electric and conventional vehicles. *European Journal of Operational Research*, 245(1):81-99.
- [Khodayar et al., 2013] Khodayar, M. E., Wu, L., and Li, Z. (2013). Electric vehicle mobility in transmission-constrained hourly power generation scheduling. *IEEE Transactions on Smart Grid*, 4(2):779-788.
- [Kirschen and Strbac, 2004] Kirschen, D. S. and Strbac, G. (2004). *Fundamentals of Power System Economics*. John Wiley & Sons, first edition.
- [Le et al., 2015] Le, T., Kovács, P., Walton, N., Vu, H. L., Andrew, L. L. H., and Hoogendoorn, S. S. P. (2015). Decentralized signal control for urban road networks. *Transportation Research Part C: Emerging Technologies*, 58:431-47

References

- [Leighton et al., 1995] Leighton, T., Makedon, F., Plotkin, S., Stein, C., Tardos, E., and Tragoudas, S. (1995). Fast approximation algorithms for multicommodity flow problems. *Journal of Computer and System Sciences*, 50(2):228–243.
- [Levin et al., 2017] Levin, M. W., Kockelman, K. M., Boyles, S. D., and Li, T. (2017). A general framework for modeling shared autonomous vehicles with dynamic network-loading and dynamic ride-sharing application. *Computers, Environment and Urban Systems*, 64:373 – 383.
- [Levin et al., 2016] Levin, M. W., Li, T., Boyles, S. D., and Kockelman, K. M. (2016). A general framework for modeling shared autonomous vehicles. In *95th Annual Meeting of the Transportation Research Board*.
- [Lighthill and Whitham, 1955] Lighthill, M. J. and Whitham, G. B. (1955). On kinematic waves. II. a theory of traffic flow on long crowded roads. *Proceedings of the Royal Society of London A: Mathematical, Physical and Engineering Sciences*, 229(1178):317–345.
- [Liu et al., 2009] Liu, H., Tesfatsion, L., and A., C. A. (2009). Derivation of locational marginal prices for restructured wholesale power markets. *Journal of Energy Markets*, 2(1):3–27.
- [Maciejewski and Bischoff, 2017] Maciejewski, M. and Bischoff, J. (2017). Congestion effects of autonomous taxi fleets. *Transport*. (submitted).
- [Maciejewski et al., 2017] Maciejewski, M., Bischoff, J., Hrl, S., and Nagel, K. (2017). Towards a testbed for dynamic vehicle routing algorithms. In *International Conference on Practical Applications of Agents and Multi-Agent Systems - Workshop on the application of agents to passenger transport (PAAMS-TAAPS)*. Submitted.
- [Mitchell et al., 2010] Mitchell, W. J., Borroni-Bird, C. E., and Burns, L. D. (2010). *Reinventing the automobile: Personal urban mobility for the 21st century*. MIT Press.
- [Mittelmann, 2016] Mittelmann, H. D. (2016). Decision tree for optimization software.
- [Mitzenmacher and Upfal, 2005] Mitzenmacher, M. and Upfal, E. (2005). *Probability and computing: Randomized algorithms and probabilistic analysis*. Cambridge University Press.
- [Neuburger, 1971] Neuburger, H. (1971). The economics of heavily congested roads. *Transportation Research*, 5(4):283–293.
- [OECD, 2014] OECD (2014). The cost of air pollution - health impacts of road transport. Technical report, Organisation for Economic Co-operation and Development (OECD).
- [O’Neill et al., 2011] O’Neill, R. P., Dautel, T., and Krall, E. (2011). Recent ISO software enhancements and future software and modeling plans. Technical report, Federal Energy Regulatory Commission.
- [Osorio and Bierlaire, 2009] Osorio, C. and Bierlaire, M. (2009). An analytic finite capacity queueing network model capturing the propagation of congestion and blocking. *European Journal of Operational Research*, 196(3): 996–1007.
- [Overbye et al., 2004] Overbye, T. J., Cheng, X., and Sun, Y. (2004). A comparison of the AC and DC power flow models for LMP calculations. In *Hawaii International Conference on System Sciences*.
- [Papageorgiou et al., 1991] Papageorgiou, M., Hadj-Salem, H., and Blosseville, J.-M. (1991). ALINEA: A local feedback control law for on-ramp metering. *Transportation Research Record: Journal of the Transportation Research Board*, (1320):58–64.
- [Pavone et al., 2011] Pavone, M., Smith, S. L., Frazzoli, E., and Rus, D. (2011). Load balancing for Mobility-on-Demand systems. In *Robotics: Science and Systems*.
- [Pavone et al., 2012] Pavone, M., Smith, S. L., Frazzoli, E., and Rus, D. (2012). Robotic load balancing for Mobility-on-Demand systems. *Int. Journal of Robotics Research*, 31(7):839–854.
- [Peeta and Mahmassani, 1995] Peeta, S. and Mahmassani, H. S. (1995). System optimal and user equilibrium time-dependent traffic assignment in congested networks. *Annals of Operations Research*, 60(1):81–113.
- [Pérez et al., 2010] Pérez, J., Seco, F., Milanés, V., Jiménez, A., Díaz, J. C., and De Pedro, T. (2010). An RFID-based intelligent vehicle speed controller using active traffic signals. *Sensors*, 10(6):5872–5887.
- [Pourazarm et al., 2016] Pourazarm, S., Cassandras, C. G., and Wang, T. (2016). Optimal routing and charging of energy-limited vehicles in traffic networks. *Int. Journal of Robust and Nonlinear Control*, 26(6):1325–1350.
- [Raghavan and Tompson, 1987] Raghavan, P. and Tompson, C. D. (1987). Randomized rounding: A technique for provably good algorithms and algorithmic proofs. *Combinatorica*, 7(4):365–374.

References

- [Rossi et al., 2017a] Rossi, F., Iglesias, R., Zhang, R., and Pavone, M. (2017a). Congestion-aware randomized routing in autonomous mobility-on-demand systems. Extended version available at <https://asl.stanford.edu/wp-content/papercite-data/pdf/Rossi.Iglesias.Zhang.Pavone.CDC17.pdf>.
- [Rossi et al., 2017b] Rossi, F., Zhang, R., Hindy, Y., and Pavone, M. (2017b). Routing autonomous vehicles in congested transportation networks: structural properties and coordination algorithms. *Autonomous Robots*. Submitted.
- [Rotering and Ilic, 2011] Rotering, N. and Ilic, M. (2011). Optimal charge control of plug-in hybrid electric vehicles in deregulated electricity markets. *IEEE Transactions on Power Systems*, 26(3):1021–1029.
- [Seow et al., 2010] Seow, K. T., Dang, N. H., and Lee, D. H. (2010). A collaborative multiagent taxi-dispatch system. *IEEE Transactions on Automation Sciences and Engineering*, 7(3):607–616.
- [Sioshansi, 2012] Sioshansi, R. (2012). OR Forum—modeling the impacts of electricity tariffs on plug-in hybrid electric vehicle charging, costs, and emissions. *Operations Research*, 60(3):506–516.
- [Smith et al., 2013] Smith, S. L., Pavone, M., Schwager, M., Frazzoli, E., and Rus, D. (2013). Rebalancing the rebalancers: Optimally routing vehicles and drivers in Mobility-on-Demand systems. In *American Control Conference*.
- [Spieser et al., 2014] Spieser, K., Treleaven, K., Zhang, R., Frazzoli, E., Morton, D., and Pavone, M. (2014). Toward a systematic approach to the design and evaluation of Autonomous Mobility-on-Demand systems: A case study in Singapore. In *Road Vehicle Automation*. Springer.
- [Srinivasan, 1999] Srinivasan, A. (1999). A survey of the role of multicommodity flow and randomization in network design and routing. In *Randomization Methods in Algorithm Design*.
- [Stott et al., 2009] Stott, B., Jardim, J., and Alsac, O. (2009). DC power flow revisited. *IEEE Transactions on Power Systems*, 24(3):1290–1300.
- [Templeton, 2010] Templeton, B. (2010). Traffic congestion & capacity. Available at <http://www.templetons.com/brad/robocars/congestion.html>.
- [Treiber et al., 2000] Treiber, M., Hennecke, A., and Helbing, D. (2000). Microscopic simulation of congested traffic. In *Traffic and Granular Flow '99*. Springer Berlin Heidelberg.
- [Treleaven et al., 2011] Treleaven, K., Pavone, M., and Frazzoli, E. (2011). An asymptotically optimal algorithm for pickup and delivery problems. In *Proc. IEEE Conf. on Decision and Control*.
- [Treleaven et al., 2012] Treleaven, K., Pavone, M., and Frazzoli, E. (2012). Models and efficient algorithms for pickup and delivery problems on roadmaps. In *Proc. IEEE Conf. on Decision and Control*.
- [Treleaven et al., 2013] Treleaven, K., Pavone, M., and Frazzoli, E. (2013). Asymptotically optimal algorithms for one-to-one pickup and delivery problems with applications to transportation systems. *IEEE Transactions on Automatic Control*, 58(9):2261–2276.
- [Turitsyn et al., 2010] Turitsyn, K., Sinitzyn, N., Backhaus, S., and Chertkov, M. (2010). Robust broadcast-communication control of electric vehicle charging. In *IEEE International Conference on Smart Grid Communications (SmartGridComm)*.
- [Tushar et al., 2012] Tushar, W., Saad, W., Poor, H. V., and Smith, D. B. (2012). Economics of electric vehicle charging: A game theoretic approach. *IEEE Transactions on Power Systems*, 3(4):1767–1778.
- [United States Census Bureau, 2017] United States Census Bureau (2017). American Community Survey. Commuting in the United States: 2009. Supplemental Table B: Time of Departure. Available at <https://www.census.gov/hhes/commuting/data/commuting.html>.
- [Urmson, 2014] Urmson, C. (2014). Just press go: Designing a self-driving vehicle. Available at <http://googleblog.blogspot.com/2014/05/just-press-go-designing-self-driving.html>.
- [U.S. Department of Transportation, 2015] U.S. Department of Transportation (2015). Revised departmental guidance on valuation of travel time in economic analysis. Technical report.
- [Wang et al., 2010] Wang, L., Lin, A., and Chen, Y. (2010). Potential impact of recharging plug-in hybrid electric vehicles on locational marginal prices. *Naval Research Logistics*, 57(8):686–700.
- [Wardrop, 1952] Wardrop, J. G. (1952). Some theoretical aspects of road traffic research. *Proceedings of the Institution of Civil Engineers*, 1(3):325–362.
- [Wilkie et al., 2014] Wilkie, D., Baykal, C., and Lin, M. C. (2014). Participatory route planning. In *ACM SIGSPATIAL*.
- [Wilkie et al., 2011] Wilkie, D., van den Berg, J. P., Lin, M. C., and Manocha, D. (2011). Self-aware traffic route planning. In *Proc. AAAI Conf. on Artificial Intelligence*.
- [World Health Organization (WHO), 2014] World Health Organization (WHO) (2014). 7 million premature deaths annually linked to air pollution. <http://www.who.int/mediacentre/news/releases/2014/air-pollution/en/>.

References

[Xiao et al., 2015] Xiao, N., Frazzoli, E., Luo, Y., Li, Y., Wang, Y., and Wang, D. (2015). Through-put optimality of extended back-pressure traffic signal control algorithm. In *Mediterranean Conf. on Control and Automation*.

[Yang and Koutsopoulos, 1996] Yang, Q. and Koutsopoulos, H. N. (1996). A microscopic traffic simulator for evaluation of dynamic traffic management systems. *Transportation Research Part C: Emerging Technologies*, 4(3):113-129.

[Zhang and Pavone, 2015] Zhang, R. and Pavone, M. (2015). A queueing network approach to the analysis and control of Mobility-on-Demand systems. In *American Control Conference*.

[Zhang and Pavone, 2016] Zhang, R. and Pavone, M. (2016). Control of robotic Mobility-on-Demand systems: A queueing-theoretical perspective. *Int. Journal of Robotics Research*, 35(1-3):186-203.

[Zhang et al., 2016a] Zhang, R., Rossi, F., and Pavone, M. (2016a). Model predictive control of Autonomous Mobility-on-Demand systems. In *Proc. IEEE Conf. on Robotics and Automation*.

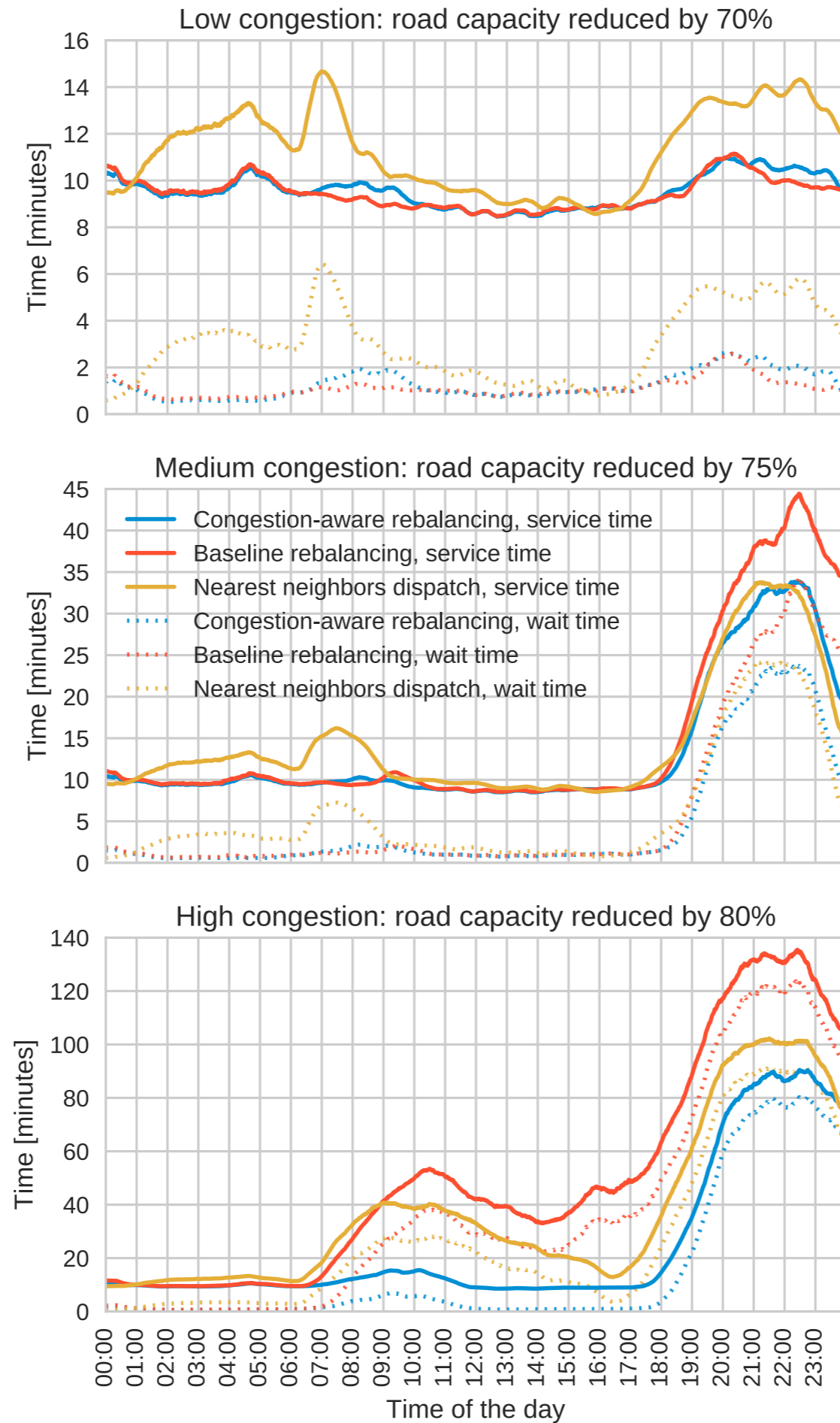
[Zhang et al., 2016b] Zhang, R., Rossi, F., and Pavone, M. (2016b). Routing autonomous vehicles in congested transportation networks: Structural properties and coordination algorithms. In *Robotics: Science and Systems*.

UPCOMING AND RECENTLY-ACHIEVED SELF-DRIVING CAR MILESTONES

- AUTOMATIC EMERGENCY BRAKING
- HIGHWAY LANE-KEEPING
- SELF-PARKING
- FULL HIGHWAY AUTONOMY
- FIRST SEX IN A SELF-DRIVING CAR
- FULL TRIPS WITH NO INPUT FROM DRIVER
- FULL TRIPS BY EMPTY CARS
- SELF-REFUELING OF EMPTY CARS
- AN EMPTY CAR WANDERING THE HIGHWAYS FOR MONTHS OR YEARS UNTIL SOMEONE NOTICES THE CREDIT CARD FUEL CHARGES
- CARS THAT READ OTHER CARS' BUMPER STICKERS BEFORE DECIDING WHETHER TO CUT THEM OFF
- AUTONOMOUS ENGINE REVVING AT RED LIGHTS
- SELF-LOATHING CARS
- AUTONOMOUS CANYON JUMPING
- CARS CAPABLE OF ARGUING ABOUT THE TROLLEY PROBLEM ON FACEBOOK

More results on congestion

Customer wait and service time



P-AMoD: full results

```
Price paid by the TSO
  coordinated: 227977.072133
  uncoordinated: 296817.428591
Unit price paid by the TSO
  coordinated: 7491.27746558
  uncoordinated: 8526.40186212
Price paid by all
  ISO only: 39604707.8459
  coordinated: 39264836.8294
  uncoordinated: 39629497.7003
Price paid by all per 100 KW
  ISO only: 7653.10996073
  coordinated: 7543.07587502
  uncoordinated: 7606.73059846
Price paid by everyone else
  ISO only: 39604707.8459
  coordinated: 39036859.7572
  uncoordinated: 39332680.2717
Price per hundred KW paid by everyone else
  ISO only: 7653.10996073
  coordinated: 7543.3804841
  uncoordinated: 7600.54406513

Cost of generation
  ISO only: 40529884.5782
  coordinated: 40756002.7821
  uncoordinated: 40917155.1849
Cost of generation per hundred KW
  ISO only: 7831.88868807
  coordinated: 7829.54027502
  uncoordinated: 7853.89153051

Price paid by all in Dallas
  ISO only: 12832491.2268
  coordinated: 12591742.8793

  uncoordinated: 12905202.0542
Price per hundred KW paid by all in Dallas
  ISO only: 7868.57561461
  coordinated: 7579.51783894
  uncoordinated: 7747.77901222
Price paid by everyone else in Dallas
  ISO only: 12832491.2268
  coordinated: 12363765.8072
  uncoordinated: 12608384.6256
Price per hundred KW paid by everyone else in Dallas
  ISO only: 7868.57561461
  coordinated: 7581.16443766
  uncoordinated: 7731.15882576
Price paid by everyone else NOT in Dallas
  ISO only: 26772216.6191
  coordinated: 26673093.95
  uncoordinated: 26724295.6461
Price per hundred KW paid by everyone else NOT in Dallas
  ISO only: 7553.96209363
  coordinated: 7525.99396176
  uncoordinated: 7540.44086681
Price paid by all at charging nodes
  ISO only: 2243271.04358
  coordinated: 2390693.73131
  uncoordinated: 2501941.65175
Price per hundred KW paid by all at charging nodes
  ISO only: 7862.43259969
  coordinated: 7571.53715428
  uncoordinated: 7815.47304232
Price paid by everyone else at charging nodes
  ISO only: 2243271.04358
  coordinated: 2162716.65918
  uncoordinated: 2205124.22316
Price per 100 KW paid by everyone else at charging nodes
  ISO only: 7862.43259969
  coordinated: 7580.09782801
  uncoordinated: 7728.73194622
```

Suboptimal Linear model

minimize
 $f_m, \lambda_m^{c, \text{in}}, \lambda_m^{c, t, \text{out}}, N_F, \theta, p$

$$V_D \left(\sum_{(\mathbf{v}, \mathbf{w}) \in \mathcal{E}} d_{v_{\mathbf{v}}, v_{\mathbf{w}}} \sum_{m=0}^M f_m(\mathbf{v}, \mathbf{w}) \right) + \sum_{t=1}^T \sum_{g \in \mathcal{G}} o_g(t) p(g, t)$$

subject to

$$\lambda_m^{t, c, \text{out}} = \begin{cases} \lambda_m^{c + c_{v_m \rightarrow w_m}, \text{in}} & \text{if } t_m = t - t_{v_m \rightarrow w_m} \\ 0 & \text{otherwise} \end{cases}$$

$$\forall t \in \{1, \dots, T\}, c \in \{1, \dots, C\}, m \in \{1, \dots, M\},$$

$$\sum_{c=1}^C \lambda_m^{c, \text{in}} = \lambda_m, \quad \forall m \in \{1, \dots, M\},$$

$$\sum_{t=1}^T \sum_{c=1}^C \lambda_m^{t, c, \text{out}} = \lambda_m, \quad \forall m \in \{1, \dots, M\},$$

$$\sum_{\mathbf{u}: (\mathbf{u}, \mathbf{v}) \in \mathcal{E}} f_0(\mathbf{u}, \mathbf{v}) + \sum_{m=1}^M 1_{v_{\mathbf{v}}=w_m} \lambda_m^{t_{\mathbf{v}}, c_{\mathbf{v}}, \text{out}} + N_I(\mathbf{v})$$

$$= \sum_{\mathbf{w}: (\mathbf{v}, \mathbf{w}) \in \mathcal{E}} f_0(\mathbf{v}, \mathbf{w}) + \sum_{m=1}^M 1_{v_{\mathbf{v}}=v_m} 1_{t_{\mathbf{v}}=t_m} \lambda_m^{c_{\mathbf{v}}, \text{in}} + N_F(\mathbf{v}), \quad \forall \mathbf{v} \in \mathcal{V},$$

$$\sum_{c_{\mathbf{v}}=1}^M \left(\sum_{m=0}^M f_m(\mathbf{v}, \mathbf{w}) \right) \leq \bar{f}_{(v_{\mathbf{v}}, v_{\mathbf{w}})}, \quad \forall (v_{\mathbf{v}}, v_{\mathbf{w}}) \in \mathcal{E}_R, \forall t_{\mathbf{v}} \in \{1, \dots, T\},$$

$$\sum_{\substack{(v, w) \in \mathcal{E}_S: \\ v_{\mathbf{v}}=v_{\mathbf{w}}=s, \\ t_{\mathbf{v}} \leq t < t_{\mathbf{w}}}} \left(\sum_{m=0}^M f_m(\mathbf{v}, \mathbf{w}) \right) \leq \bar{S}_s, \quad \forall s \in \mathcal{S}, t \in \{1, \dots, T\},$$

$$\sum_{(u, v) \in \mathcal{E}_P} \frac{\theta(u, t) - \theta(v, t)}{x_{u, v}} + 1_{v \in \mathcal{G}} p(v, t) = 1_{v \in \mathcal{L}} d_v(t) + \sum_{(v, w) \in \mathcal{E}_P} \frac{\theta(v, t) - \theta(w, t)}{x_{v, w}},$$

$$\forall v \in \mathcal{B}, t \in \{1, \dots, T\},$$

$$-\bar{p}_{b_1, b_2} \leq \frac{\theta(b_1, t) - \theta(b_2, t)}{x_{b_1, b_2}} \leq \bar{p}_{b_1, b_2}, \quad \forall (b_1, b_2) \in \mathcal{E}_P, t \in \{1, \dots, T\},$$

$$\underline{p}_g(t) \leq p(g, t) \leq \bar{p}_g(t), \quad \forall g \in \mathcal{G}, t \in \{1, \dots, T\},$$

$$-p_g^-(t) \leq p(g, t+1) - p(g, t) \leq p_g^+(t), \quad \forall g \in \mathcal{G}, t \in \{1, \dots, T-1\},$$

$$d_l(t) \leq \bar{d}_l(t), \quad \forall l \in \mathcal{L}, t \in \{1, \dots, T\},$$

$$d_l(t) = d_{l, e}(t) + J_C \delta c_{M_{P, R}(l)}^+ \sum_{(\mathbf{v}, \mathbf{w}) \in M_{P, G}^+(l, t)} \sum_{m=0}^M f_m(\mathbf{v}, \mathbf{w})$$

$$+ J_C \delta c_{M_{P, R}(l)}^- \sum_{(\mathbf{v}, \mathbf{w}) \in M_{P, G}^-(l, t)} \sum_{m=1}^M f_m(\mathbf{v}, \mathbf{w}), \quad \forall l \in \mathcal{L}, t \in \{1, \dots, T\}.$$

Dual decomposition algorithm

Algorithm 1 Dual decomposition distributed algorithm for the P-AMoD problem

$k \leftarrow 1$

ISO sets $\lambda_{\text{ISO}}^{\text{eq},k} \leftarrow$ dual solution to Economic Dispatch problem with $\{d_l\} = \{d_{l,e}\}$.

repeat

ISO informs TSO of $\lambda_{\text{ISO}}^{\text{eq},k}$

TSO sets $\{f_m^k, \lambda_m^{c,\text{in},k}, \lambda_m^{t,c,\text{out},k}, N_F^k\} \leftarrow$ solution to VRCP Problem with

$p_{(\mathbf{v},\mathbf{w})} = \lambda_{\text{ISO}}^{\text{eq},k}$

ISO sets $\{\theta^k, p^k\} \leftarrow$ solution to Lagrangian relaxation of Economic Dispatch Problem

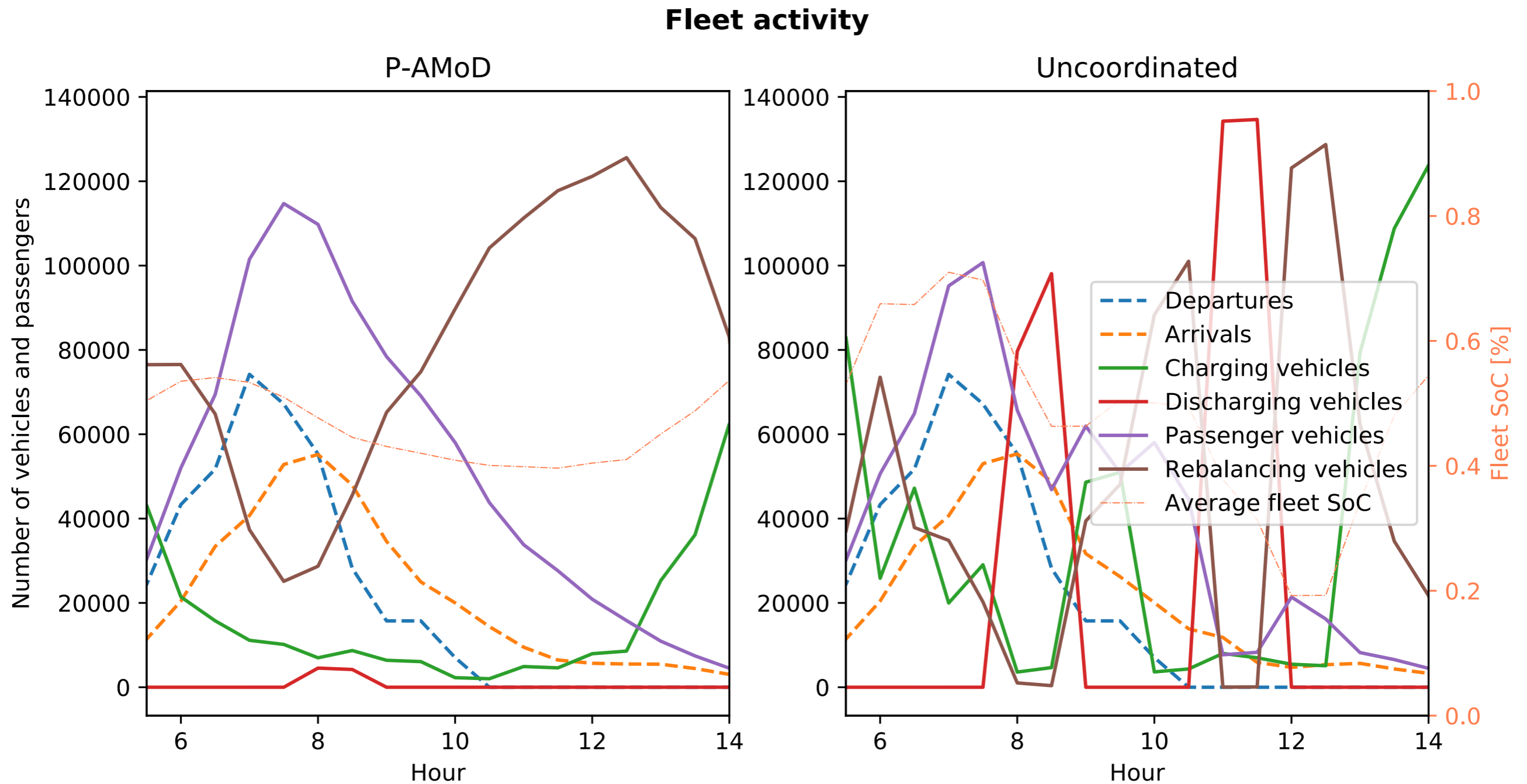
TSO informs ISO of proposed charging schedule f_m^k .

ISO updates $\lambda_{\text{ISO}}^{\text{eq},k+1} \leftarrow \lambda_{\text{ISO}}^{\text{eq},k} + \alpha_k f_{\text{ISO}}^{\text{eq}}(f_m^k, \theta^k, p^k)$

$k \leftarrow k + 1$

until $\|\lambda_{\text{ISO}}^{\text{eq},k+1} - \lambda_{\text{ISO}}^{\text{eq},k}\| \leq \varepsilon$

Fleet activity: P-AMoD vs uncoordinated

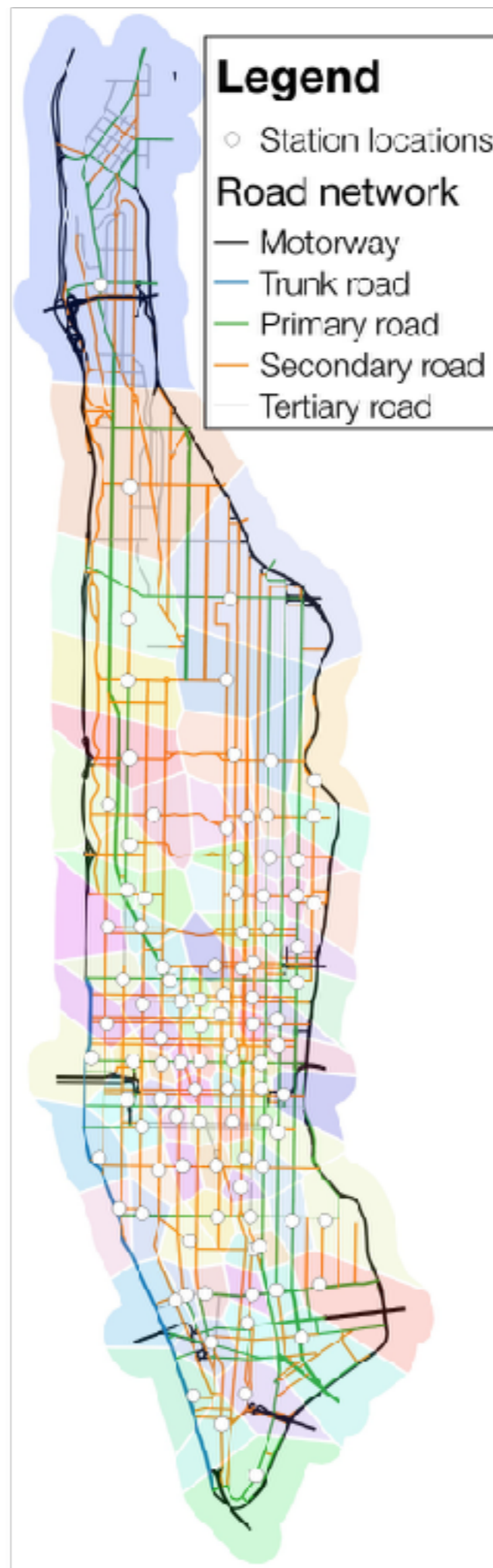


Sensitivity to node-symmetry

Table 1: Customer travel times with and without rebalancing for different levels of network asymmetry.

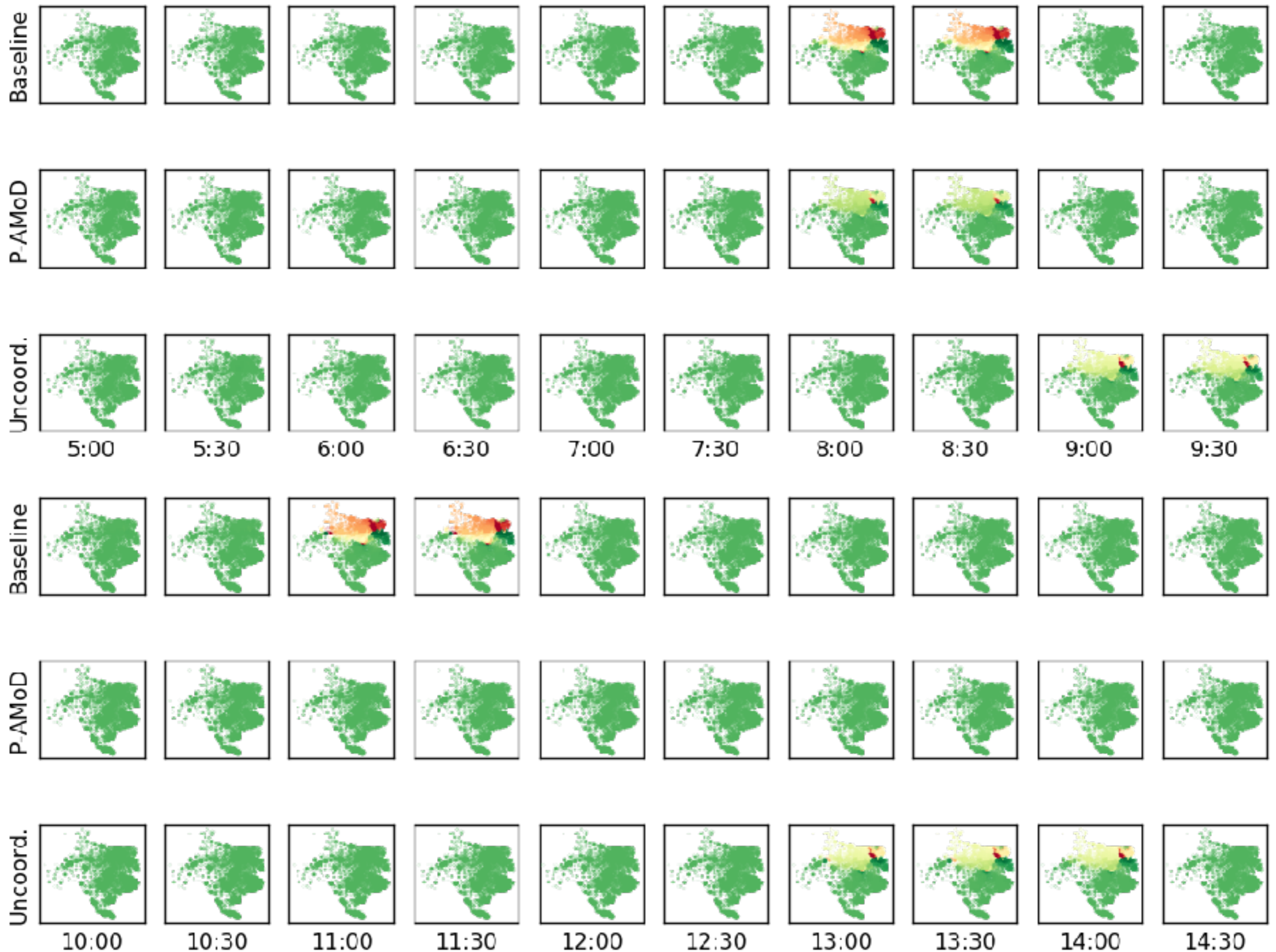
Cap. reduction	Average travel time [s]		Travel time increase
	Without reb.	With reb.	
0%	58.00	58.67	1.16 %
10%	58.12	59.15	1.76 %
20%	58.49	59.67	2.02 %
30%	59.26	60.56	2.20 %
40%	60.65	61.78	1.86 %
50%	63.66	64.55	1.40 %
60%	72.04	72.13	0.12 %

A map of

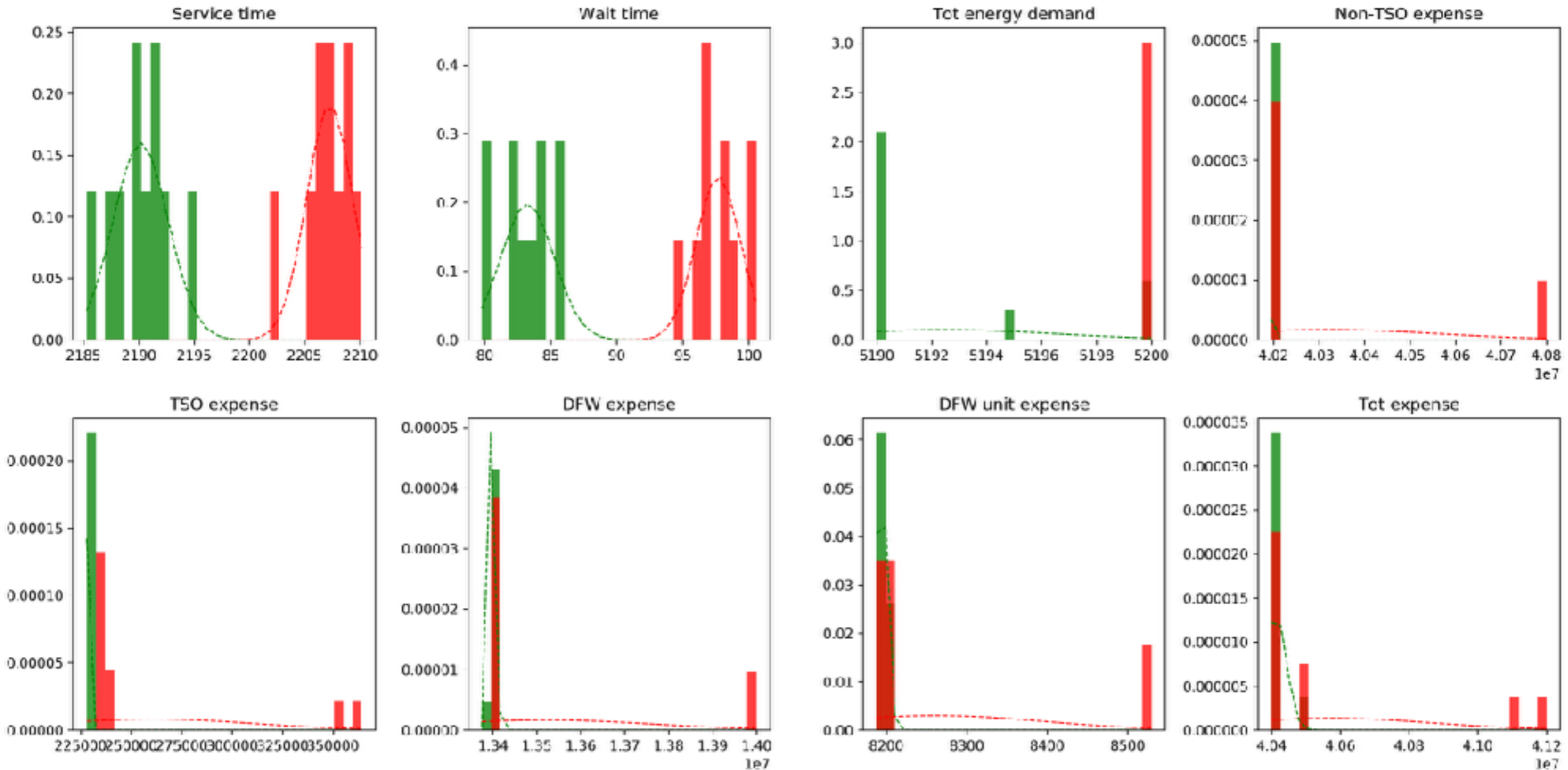


New York

Full P-AMoD results



Receding-horizon P-AMoD



Receding-horizon P-AMoD

TSO expense

